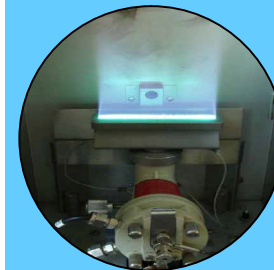
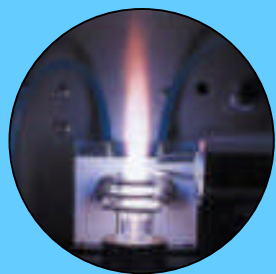
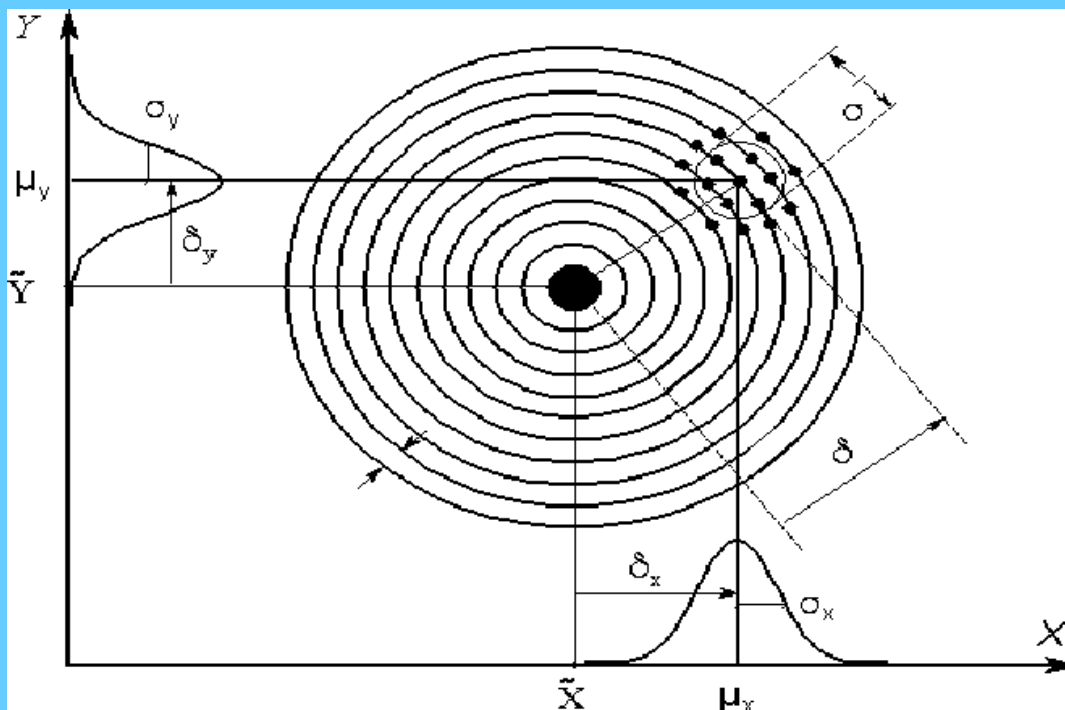


## Chemical (Elemental) Analysis

Raimund Horn

Dep. of Inorganic Chemistry, Group Functional Characterization, Fritz-Haber-Institute of the Max-Planck-Society



## **1. Introduction**

### **1.1 Concentration Ranges**

### **1.2 Accuracy and Precision**

### **1.3 Decision Limit, Detection Limit, Determination Limit**

## **2. Methods for Quantitative Elemental Analysis**

### **2.1 Chemical Methods**

#### **2.1.1 Volumetric Methods**

#### **2.1.2 Gravimetric Methods**

### **2.2 Electroanalytical Methods**

#### **2.2.1 Potentiometry**

#### **2.2.2 Polarography**

## **2.6 Spectroscopic Methods**

**2.6.1 Atomic Emission Spectroscopy**

**2.6.2 Atomic Absorption Spectroscopy**

**2.6.3 Inductively Coupled Plasma Mass Spectrometry**

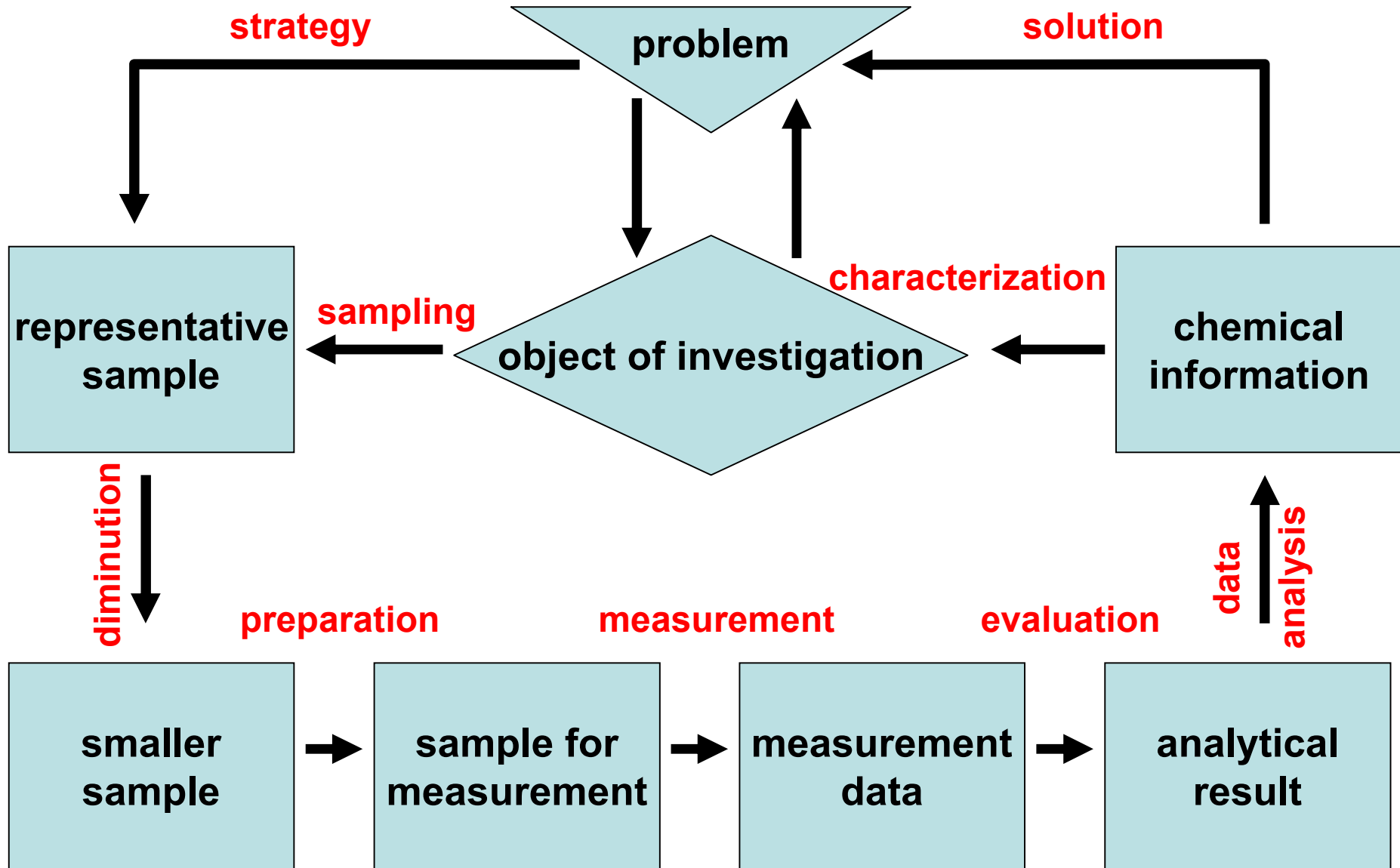
**2.6.4 X-Ray Fluorescence Spectroscopy**

**2.6.5 Electron Probe X-Ray Microanalysis**

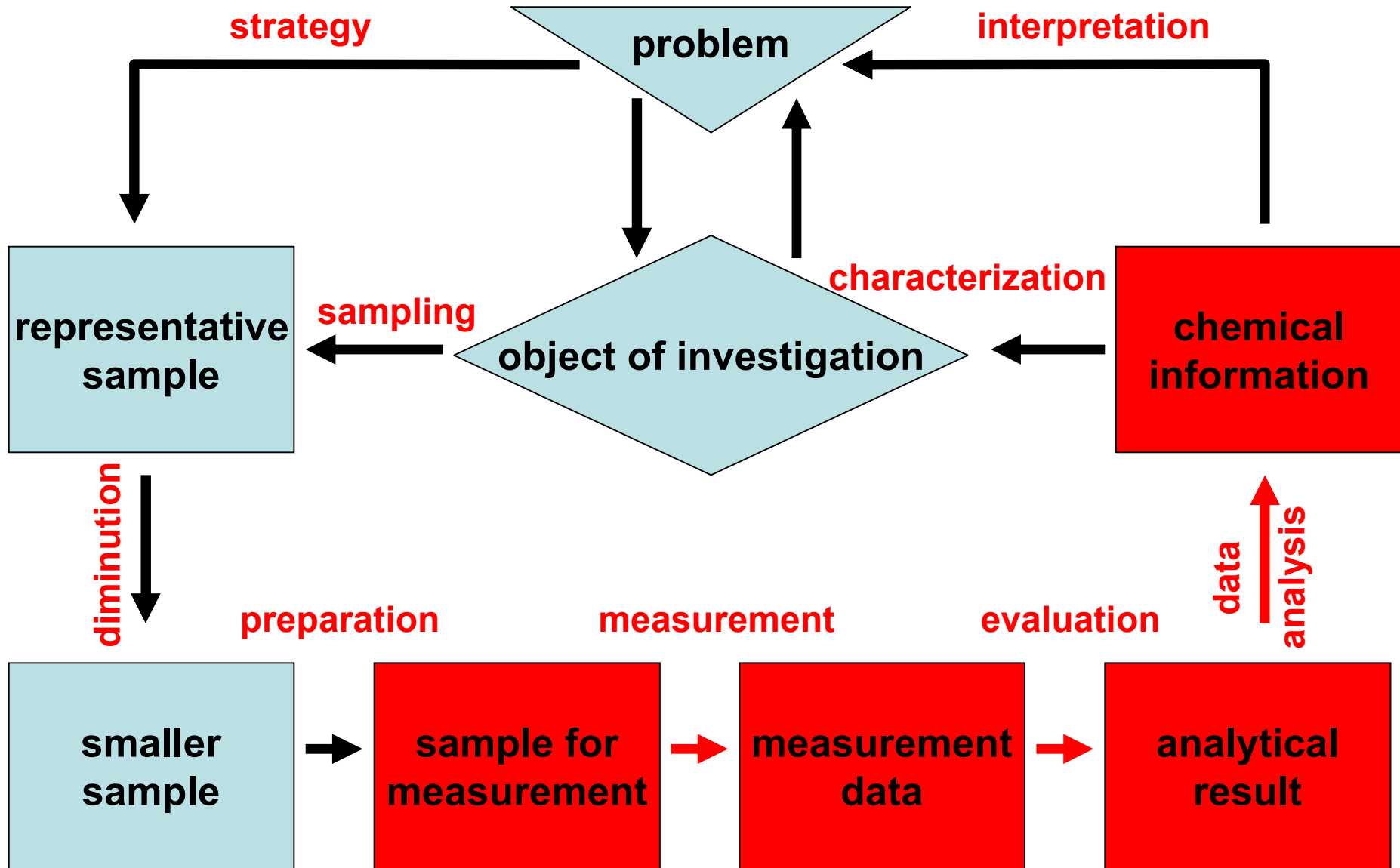
**3 Specification of an Analytical Result**

**4 Summary**

**5 Literature**







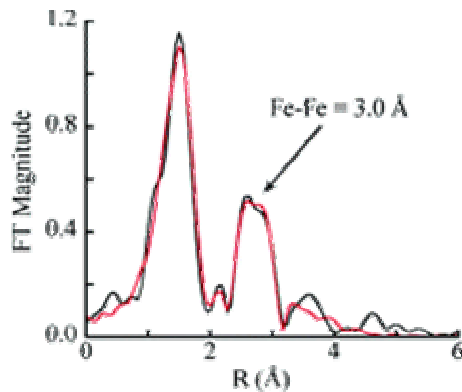
## Science

example: Determination by X-ray Absorption Spectroscopy of the Fe-Fe Separation in the Oxidized Form of the Hydroxylase of Methane Monooxygenase Alone and in the Presence of MMOD

Rudd D. J., Sazinsky M. H., Merckx M., et al. *Inorg. Chem.* **2004**, 43 (15), 4579-4589, 2004

### Motivation

fundamental interest  
future developments



## Industry

example: manufacturer of iron -  
Shall I buy this iron ore or not ?



### Motivation money

precision (e.g.)

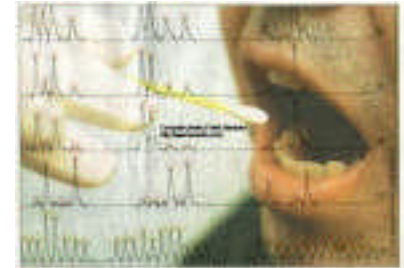
53 ± 5wt% vs. 53 ± 1wt%

accuracy (e.g.)

53 ± 1wt% vs. 51 ± 1wt%

## Law

example: Is the accused guilty  
or not guilty ?



### Motivation human fate

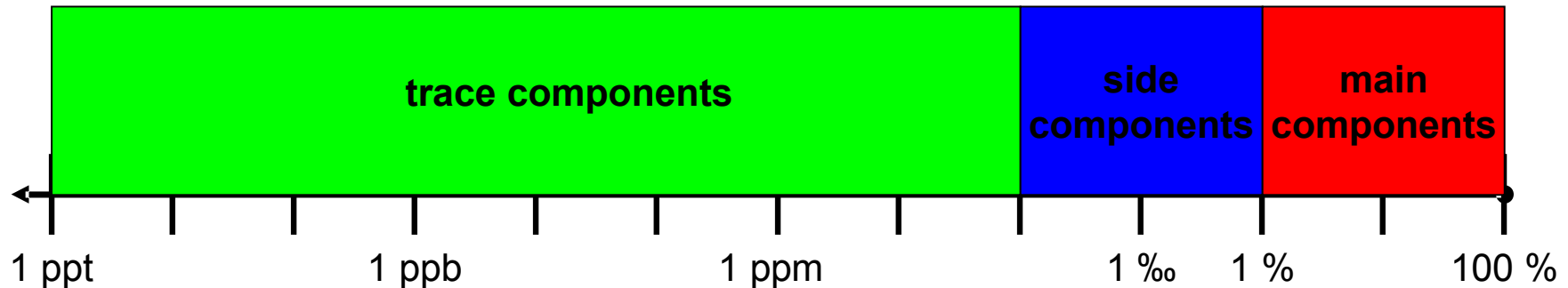
murder conviction

genetic fingerprint fits – lifelong  
prison

genetic fingerprint does not fit -  
acquittal

**consequences of the result**

### concentration ranges in elemental analysis



**ppt (w/w)**

$10^{-12}$  g/g

pg/g

ng/kg

**ppb (w/w)**

$10^{-9}$  g/g

ng/g

µg/kg

**ppm (w/w)**

$10^{-6}$  g/g

µg/g

mg/kg

**‰ (w/w)**

$10^{-3}$  g/g

mg/g

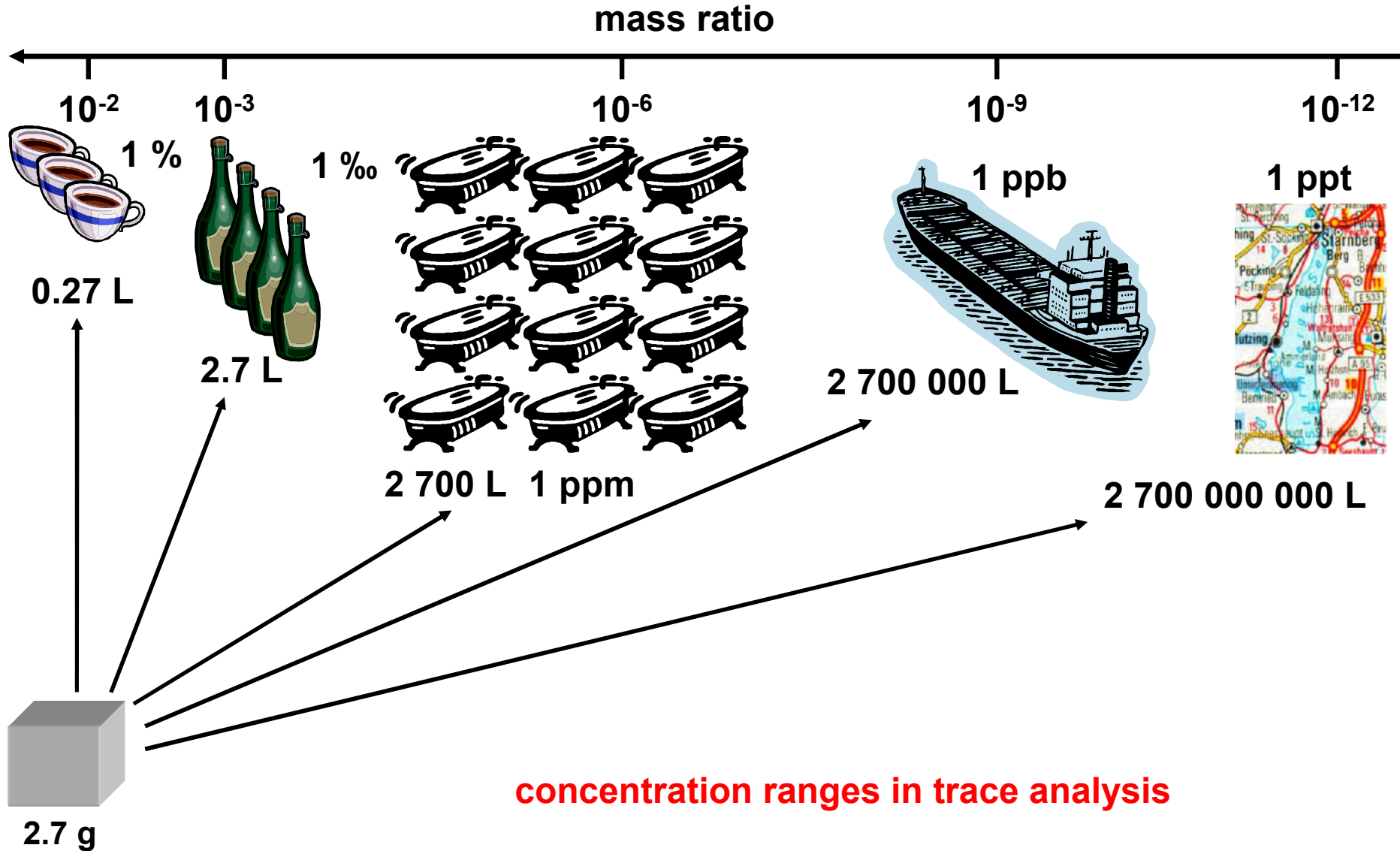
g/kg

**% (w/w)**

$10^{-2}$  g/g

0.01 g/g

10 mg/kg



## 1.2 Accuracy and Precision

### accuracy:

- can be defined as the consistency between the mean of an analytic result and the value held as the true value
- has to be verified before each analysis by means of standards
- describing quantities:

$$error_{\bar{x}} = \pm |\bar{x} - \hat{x}'|$$

$$relative\ error_{\bar{x}} = \frac{\pm |\bar{x} - \hat{x}'|}{\hat{x}'} \times 100$$

### precision (uncertainty):

- describes in a positive (negative) manner the influence of random errors on an analytic result
- describing quantities:

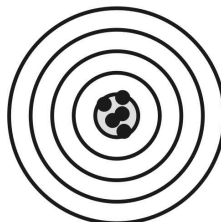
$$s = \sqrt{\frac{\sum_i (x_i - \bar{x})^2}{n - 1}}$$

**Gaussian distributed errors!**

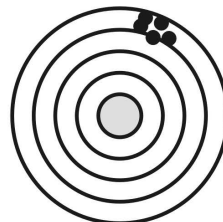
$$v = s^2 = \frac{\sum_i (x_i - \bar{x})^2}{n - 1}$$

**wrong results**

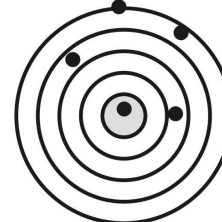
**main and side component analysis**



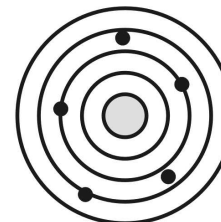
accurate and precise



precise but inaccurate



inaccurate and imprecise



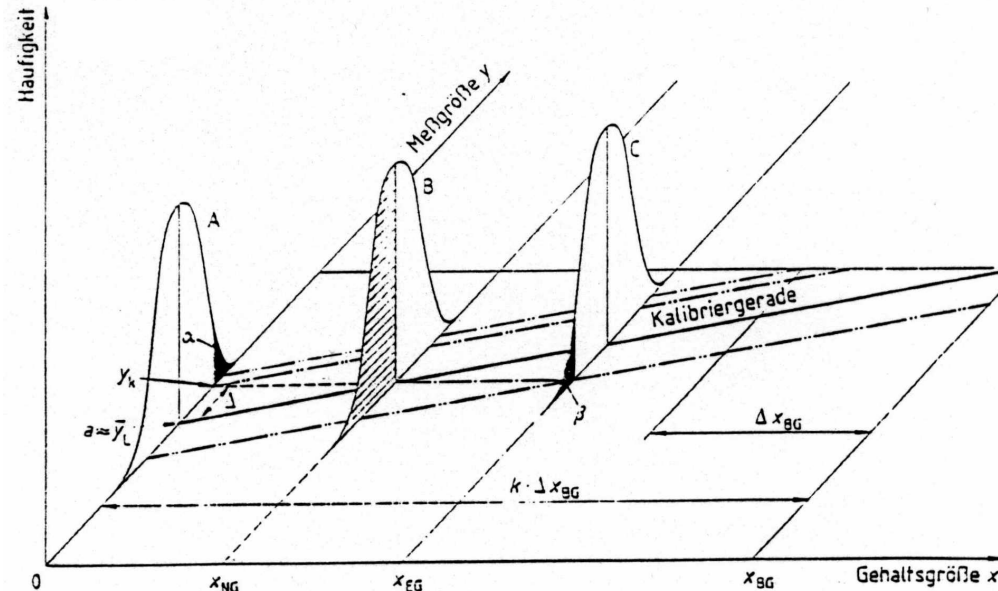
accurate but imprecise



**trace and ultra trace analysis**

## 1.3 Decision Limit, Detection Limit, Determination Limit

- the lower the concentration of an analyte, the more difficult becomes its qualitative detection and its quantification
- stochastic errors become more and more pronounced
- the decision limit and the detection limit are lower limits characterizing the performance of a method to discriminate a true value from a blank value
- the determination limit guarantees the quality of a quantitative result (user specific)



- $y_k$  Kritischer Wert der Meßgröße
- $a$  Ordinatenabschnitt der Kalibrierfunktion
- $\bar{y}_L$  Leerwert
- $\Delta$  Breite des einseitigen Prognoseintervalls
- $\Delta = \Delta a$  (Kalibriergeradenmethode)
- $\Delta = \Delta \bar{y}_L$  (Leerwertmethode)
- $\Delta x_{BG}$  Halbe Breite des zweiseitigen Prognoseintervalls der Bestimmungsgrenze
- $1/k$  Relative Ergebnisunsicherheit zur Charakterisierung der Bestimmungsgrenze
- $x_{NG}$  Nachweisgrenze
- $x_{EG}$  Erfassungsgrenze
- $x_{BG}$  Bestimmungsgrenze
- A Verteilung der Meßwerte der Leerprobe
- B Verteilung der Meßwerte einer Probe mit dem Gehalt der Nachweisgrenze
- C Verteilung der Meßwerte einer Probe mit dem Gehalt der Erfassungsgrenze

$$y_k = \bar{y}_B + \frac{t_{f,a} \times s_B}{\sqrt{n}} \quad \text{or} \quad y_k = \bar{y}_B + b x_{NG} \quad \text{or} \quad x_{NG} = \frac{t_{f,a} \times s_B}{b \times \sqrt{n}}$$

for  $a = b \quad x_{EG} = 2 \times x_{NG}$



### 2.1 Chemical Methods

- volumetric methods
- gravimetric methods

### 2.2 Electroanalytical Methods

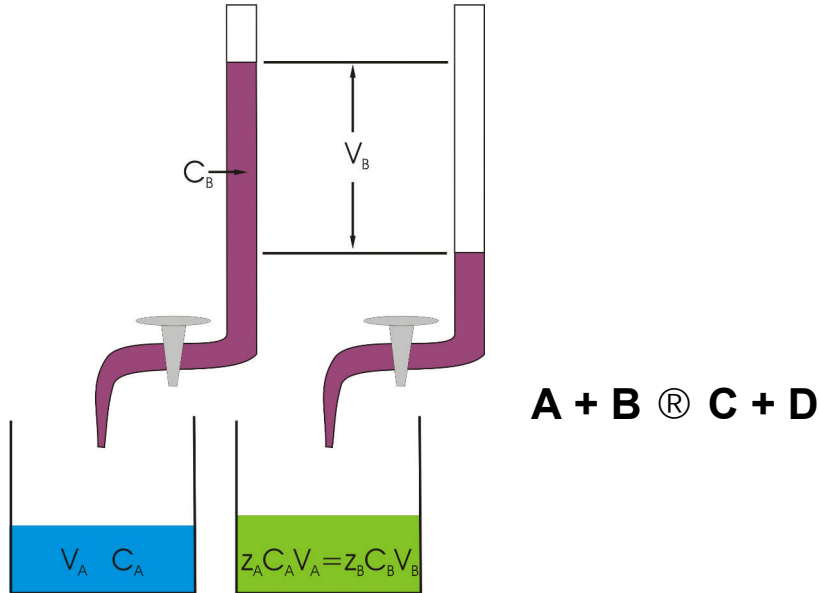
- potentiometry
- polarography

### 2.3 Spectroscopic Methods

- atomic emission
- atomic absorption
- inductively coupled plasma mass spectrometry
- X-ray fluorescence
- electron probe X-ray microanalysis

## 2.1.1 Volumetric Methods - Principle

### principle of volumetric methods



- fast, complete and stoichiometric well defined reaction
- the extend of the reaction can be monitored (e.g. pH, electric potential)
- the point of equivalence can be detected precisely (e.g. sudden color change, steep pH or potential change)

### evaluation of the result

$$p = V_B \times k \times N \times \frac{100}{m_e} \text{ in \%}$$

$p$  = percentage of the analyte in the sample

$V_B$  = volume in ml dropped in from the burette

$k$  = stoichiometric factor (mg analyte/ml)

$N$  = correction factor for the theoretical value  $k$

$e$  = weighted sample (in mg)

$$\frac{S_P}{p} = \sqrt{\frac{\frac{\partial S_{m_e}}{\partial m_e}^2}{\frac{\partial S_{m_e}}{\partial m_e}^2} + \frac{\frac{\partial S_{V_B}}{\partial V_B}^2}{\frac{\partial S_{V_B}}{\partial V_B}^2} + \frac{\frac{\partial S_N}{\partial N}^2}{\frac{\partial S_N}{\partial N}^2}}$$

inserting typical values

$$0.1\% < \frac{S_P}{p} < 1\%$$

**advantage: high precision!!!**

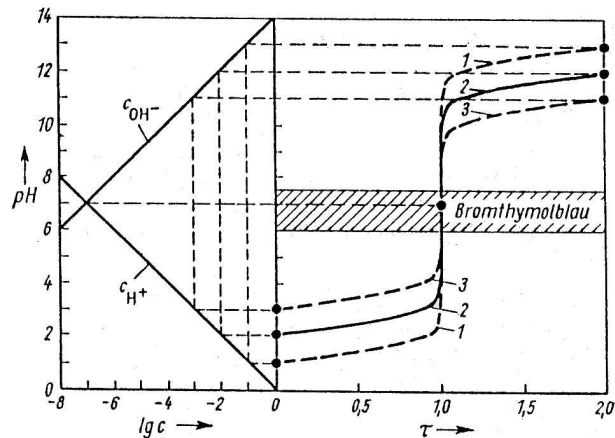


## 2.1.1 Volumetric Methods – Acid Base Titration

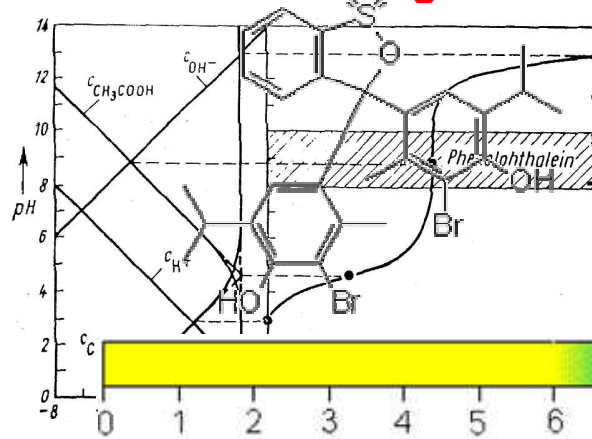
acid – base reaction:  $H_nA + nBOH \rightleftharpoons A^{n-} + nB^+ + nH_2O$  ( $z_A=n$ ,  $z_B=1$ )

titration curve: 
$$t = \frac{z_B \times C_B \times V_B}{z_A \times C_A \times V_A} = \frac{K_a}{10^{-pH} + K_a} + \frac{V_S + V}{C_S \times V_S} \times \frac{K_w}{10^{-pH}} - 10^{-pH} \quad K_w = [H^+][OH^-]$$

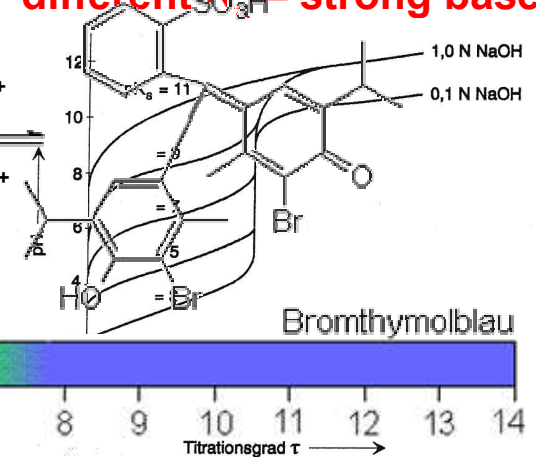
**strong acid – strong base**



**weak acid – strong base**



**different  $K_a$  – strong base**



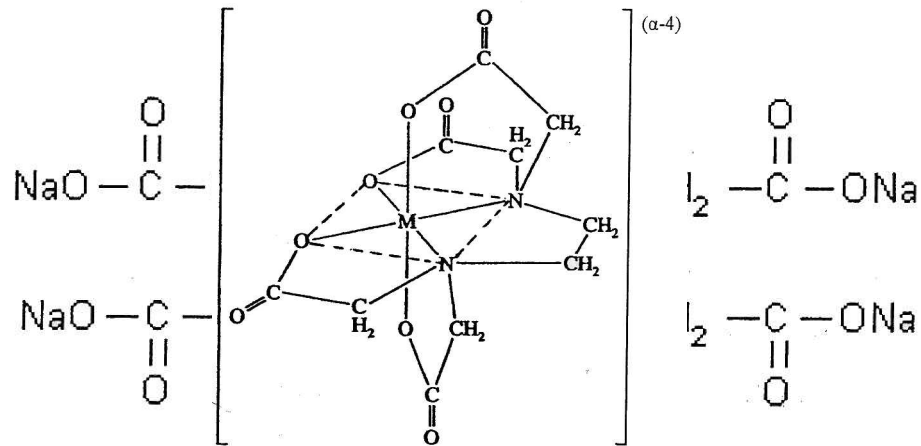
$$pH = pK_{a,Ind} \pm 1$$

- choice of the indicator depends on  $K_a$
- very weak acids (bases) can be titrated in non-aqueous solvents as liquid ammonia or 100% acetic acid

## 2.1.1 Volumetric Methods - Complexometry



most used ligand - EDTA



M-EDTA chelate

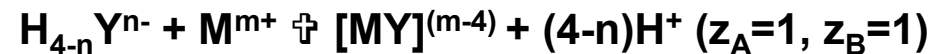
indication:  $HI^{2-} + M^{m+} \rightleftharpoons MI^{(m-3)} + H^+$   
e.g. Eriochromschwarz T

applicable for the determination of:

$Mg^{2+}$ ,  $Ca^{2+}$ ,  $Sr^{2+}$ ,  $Ba^{2+}$  at pH 8-11

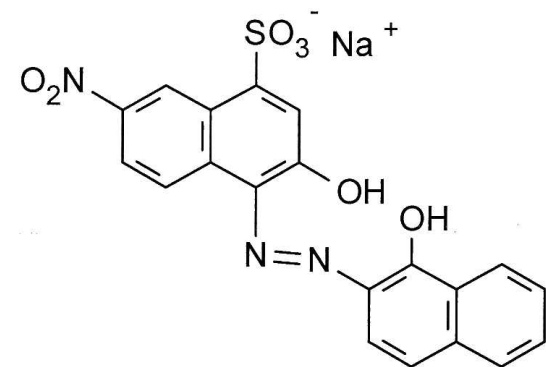
$Mn^{2+}$ ,  $Fe^{2+}$ ,  $Co^{2+}$ ,  $Ni^{2+}$ ,  $Cu^{2+}$ ,  $Zn^{2+}$ ,  $Cd^{2+}$ ,  $Al^{3+}$ ,  $Pb^{2+}$ ,  $VO^{2+}$  at pH 4-7

$Bi^{3+}$ ,  $Co^{3+}$ ,  $Cr^{3+}$ ,  $Fe^{3+}$ ,  $Ga^{3+}$ ,  $In^{3+}$ ,  $Sc^{3+}$ ,  $Ti^{3+}$ ,  $V^{3+}$ ,  $Th^{4+}$  at pH 1-4



$$[M^{m+}] = \frac{[MY^{(m-4)}]}{K_f \times [EDTA]_{total} \times a_{Y^{4-}}}$$

complex formation only with  $Y^{4-}$   
▷ buffer required



## 2.1.1 Volumetric Methods – Redox Titration

redox reaction:  $n_B \text{Ox}_B + n_A \text{Red}_A \rightleftharpoons n_B \text{Red}_B + n_A \text{Ox}_A$  ( $z_A = n_B$ ,  $z_B = n_A$ )

examples:



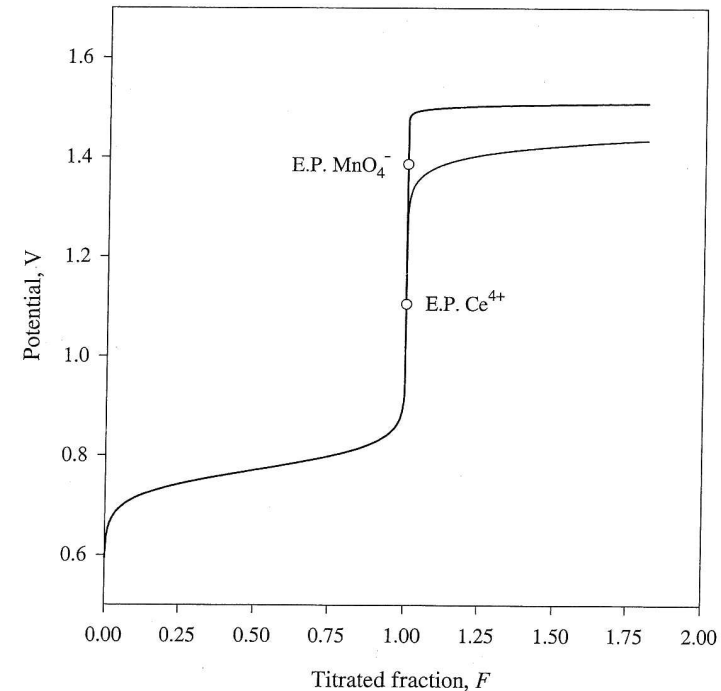
$$t = \frac{z_A \times C_A \times V_A}{z_B \times C_B \times V_B}$$

$$0 < t < 1 \quad U = U_A = U_A^0 + \frac{RT}{n_B F} \times \ln \frac{t}{1-t}$$

$$t = 1 \quad U_{eq} = \frac{n_A U_B^0 + n_B U_A^0}{n_A + n_B}$$

$$t > 1 \quad U = U_B = U_B^0 + \frac{RT}{n_A F} \times \ln(t - 1)$$

titration curve



indication: self indication (violet  $\text{MnO}_4^-$  ® colorless  $\text{Mn}^{2+}$ )  
 redox indicator ( $\text{In}_{\text{Red}} \rightleftharpoons \text{In}_{\text{Ox}} + n\text{e}^-$ )  
 potentiometric endpoint detection

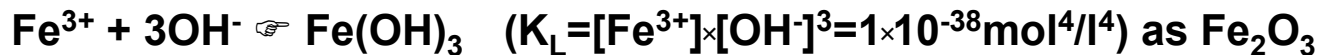
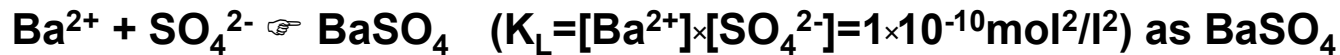
## 2.1 Chemical Methods

### 2.1.2 Gravimetric Methods

precipitation reaction:  $n_+ M^{z+}(aq) + n_- A^{z-}(aq) \ll M_{n_+} A_{n_-}(s)$

- precipitation of the ion to be determined by a suitable precipitating agent
- filtering and washing of the precipitate
- transformation into a compound of well defined stoichiometry (drying/calcination)
- ® weighing

examples



$$[M^{z+}] = \sqrt[n_+ + n_-]{K_L \frac{n_-}{n_+} \frac{\bar{c}^{n_-}}{\bar{c}^{n_+}}} \quad [A^{z-}] = \sqrt[n_+ + n_-]{K_L \frac{n_+}{n_-} \frac{\bar{c}^{n_+}}{\bar{c}^{n_-}}}$$

➤ for analytical purposes:  $a_p = 1 - \frac{[M^{z+}] \times V}{[M^{z+}]_0 \times V_0} \approx 0.997$

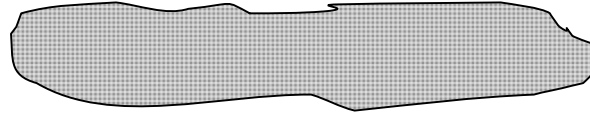
➤ advantage

▷ one of the most precise analytical methods

$$\frac{s_m}{m} = \sqrt{\frac{n_-}{n_+} \frac{s_{m_e}}{m_e} \frac{\bar{c}^{n_-}}{\bar{c}^{n_+}} + \frac{n_+}{n_-} \frac{s_{m_a}}{m_a} \frac{\bar{c}^{n_+}}{\bar{c}^{n_-}}} \quad 0.01\% < \frac{s_m}{m} < 0.1\%$$

electrode reaction,  $I_{\text{Faraday}} = 0$  (potentiometry)

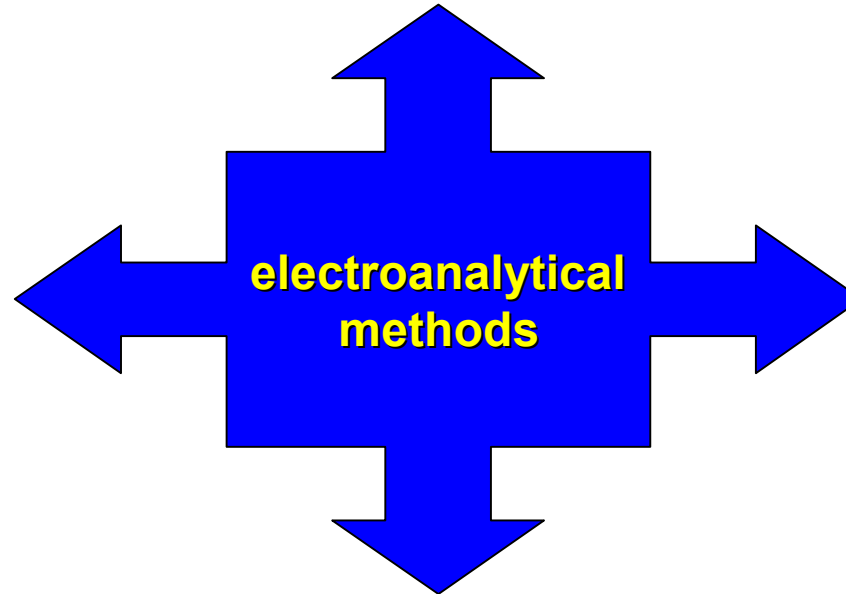
➤ ion-selective electrodes



electrode reaction, DC,  
 $I_{\text{Faraday}} \neq 0$  (voltametry)



➤ coulometry



no electrode  
reaction, AC, high  
frequency

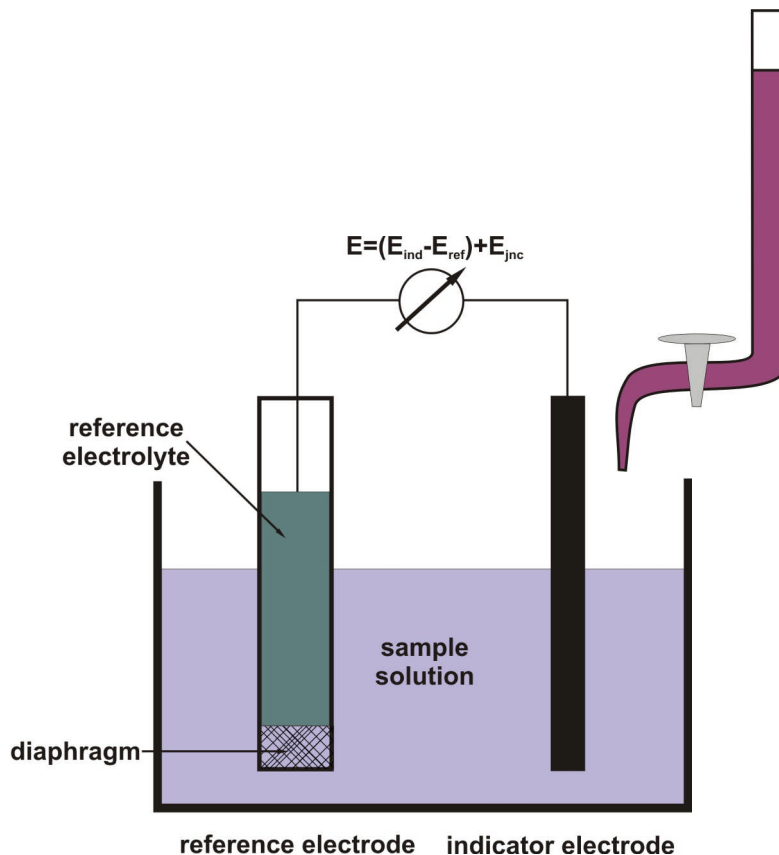
➤ conductometry

electrode reaction, AC,  
 $I_{\text{Faraday}} \neq 0$

➤ AC polarography

### 2.2.1 potentiometry, potentiometric titration

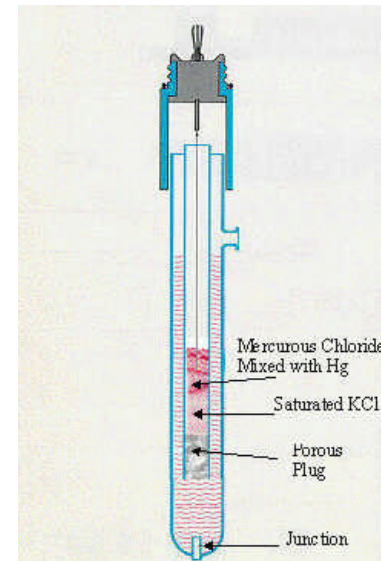
- principle ⊃ measurement of the cell potential (potential between two electrodes at zero current)
- relation of the cell potential and the analyte concentration



typical reference electrode  
calomel electrode



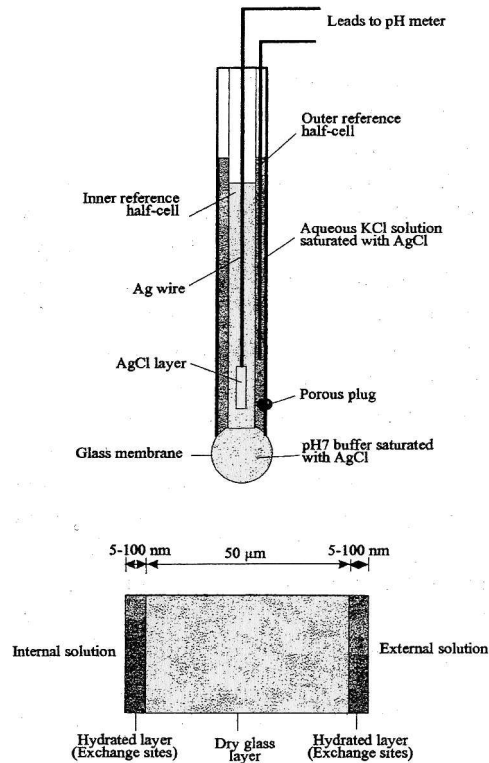
$$E = E^{0'} - \frac{0.05916\text{V}}{2} \log[\text{Cl}^-]^2$$



- electrolyte = saturated KCl solution (3.8mol/l at 25°C) ⊃  $[\text{Cl}^-] = \text{constant}$   
⊃ ref. pot.  $E = \text{const.}$

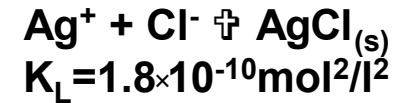
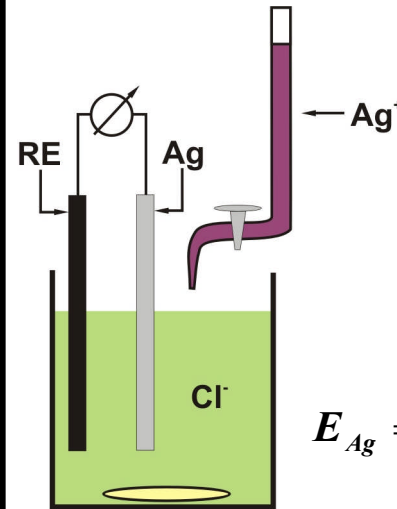
### 2.2.1 Potentiometry, Potentiometric Titration

#### pH measurement with the glass electrode



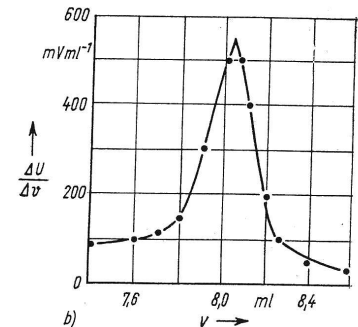
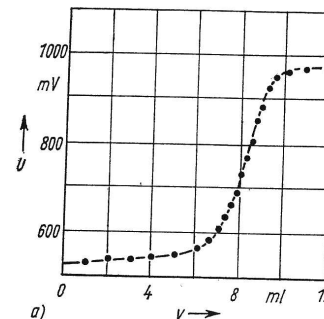
$$E = D_j_{As} + D_j_{Diff} + \frac{RT}{F} \ln 10 \times (pH_{in} - pH_{out})$$

#### Cl<sup>-</sup> determination with a silver electrode



$$E_{Ag} = E^0_{Ag/Ag^+} - \frac{2.303RT}{1 \times F} \log \frac{1}{a_{Ag^+}}$$

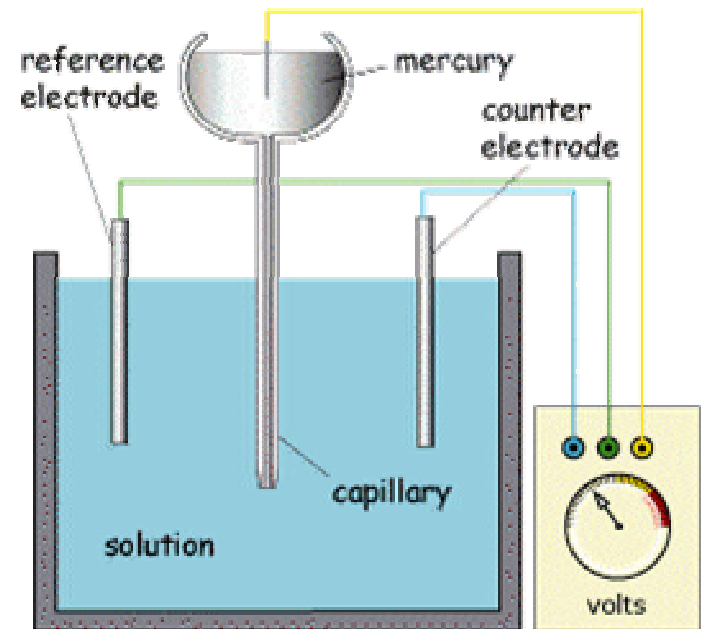
$$E_{Ag} = E^0_{Ag/Ag^+} + 0.059 \log K_L - 0.059 \log [Cl^-]$$



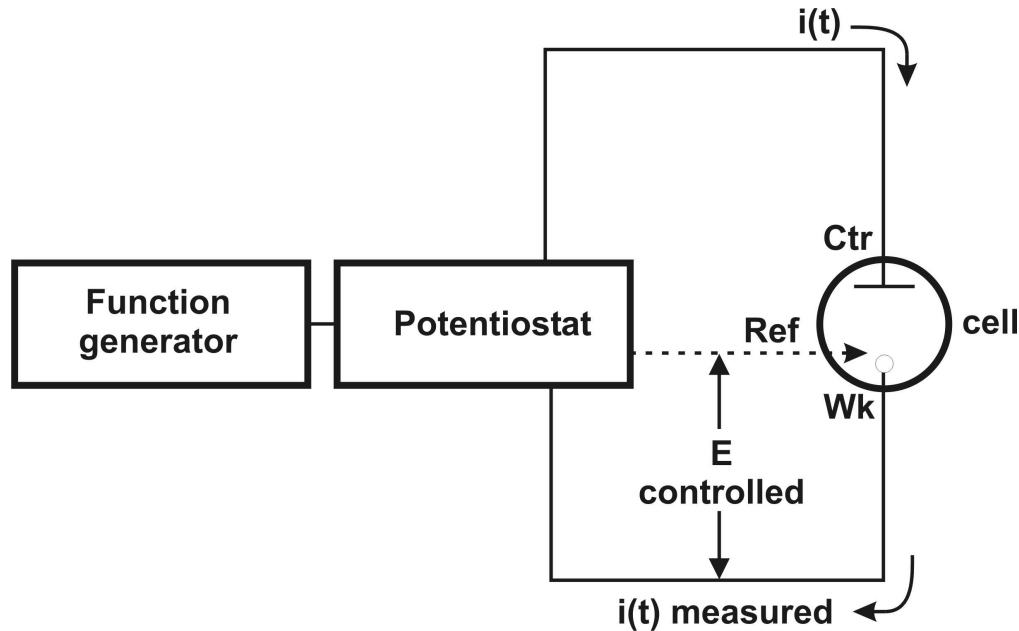
- measurement of current – voltage curves (voltametry) gives information of the chemical composition and the concentration of the analytes in the sample (working range  $1 \times 10^{-6} < c_A < 1 \times 10^{-3} \text{ mol/l}$ )
- polarography was invented in 1922 by Jaroslav Heyrovsky (Nobelprice 1959)

- a polarographic cell contains:
  - a polarizable working electrode (dropping mercury electrode)
  - a non-polarizable counter electrode (e.g. Pt wire)
  - a reference electrode (e.g. calomel electrode)
  - a supporting electrolyte (e.g.  $\text{Li}^+ \text{Cl}^-$  in  $\text{H}_2\text{O}$ )

### electrode arrangement for polarographic measurements

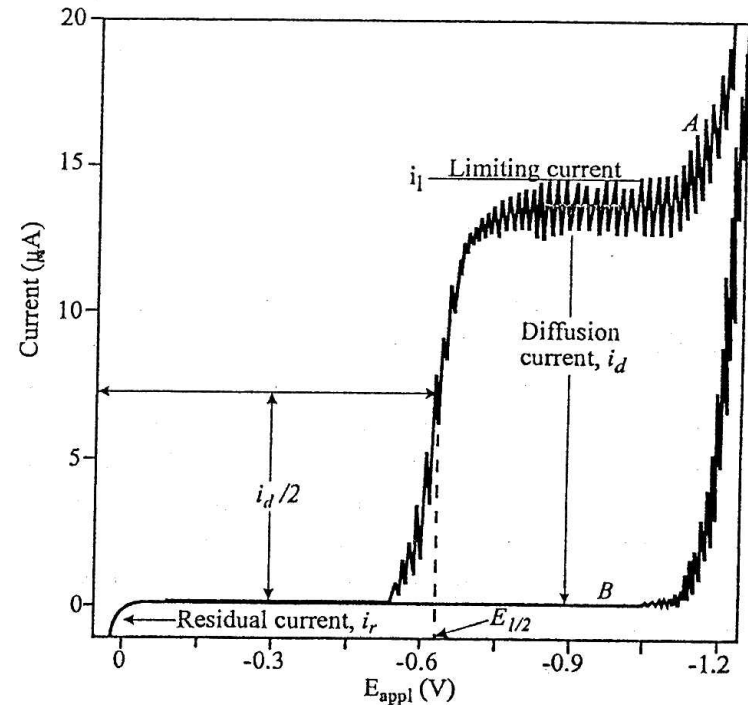






- half step potential ( $E_{1/2}$ ) characteristic for the analyte
- height of the step ( $i_d/2$ ) proportional to the concentration of the analyte
- working potential range  $-2.2\text{V} < E_{\text{appl}} < 0.3\text{V}$
- applicable to reducible or oxidizable metal ions or organic compounds

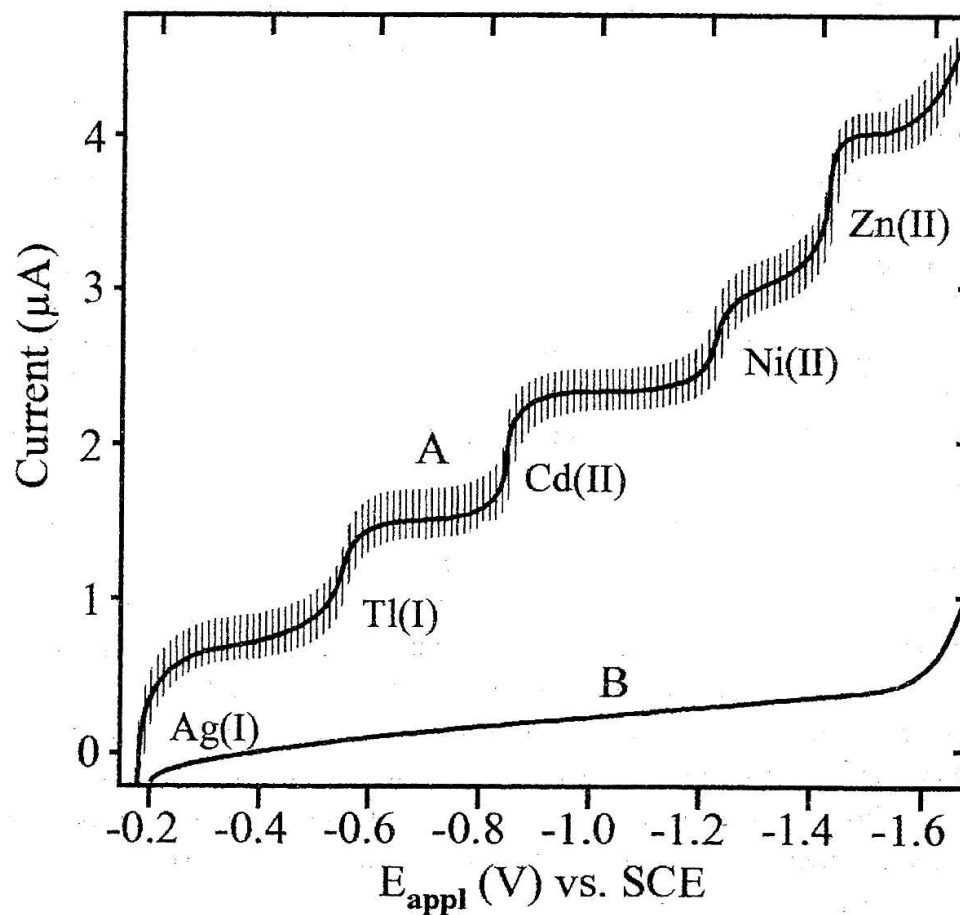
#### example: Cd determination



**A:**  $5 \times 10^{-4}$  mol  $\text{Cd}^{2+}$  in 1 mol/l HCl as supporting electrolyte

**B:** pure supporting electrolyte

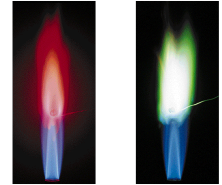
#### polarographic oligo-element determination



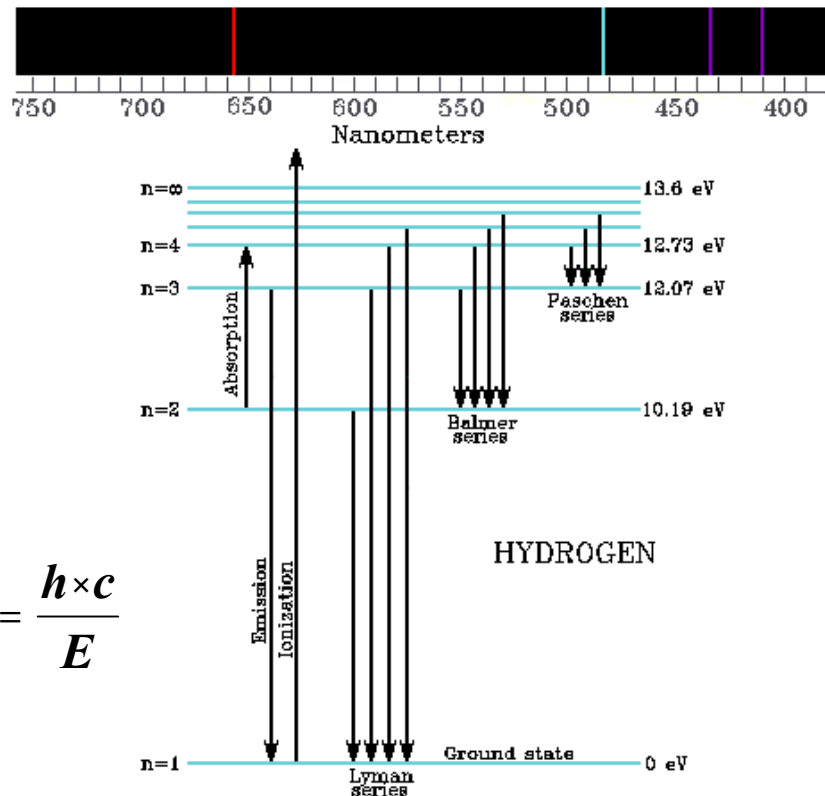
**A:**  $1 \times 10^{-4}$  mol/l  $\text{Ag}^+$ ,  $\text{Tl}^+$ ,  $\text{Cd}^{2+}$ ,  $\text{Ni}^{2+}$ ,  $\text{Zn}^{2+}$  in 1 mol/l  $\text{NH}_3$  and 1 mol/l  $\text{NH}_4\text{Cl}$  supporting electrolyte

**B:** pure supporting electrolyte

- history: one of the oldest methods for elemental analysis (flame emission - Bunsen, Kirchhoff 1860)
- principle: recording of line spectra emitted by excited atoms or ions during radiative de-excitation (valence electrons)



#### optical transitions and emission spectrum of H



#### intensity of an emission line

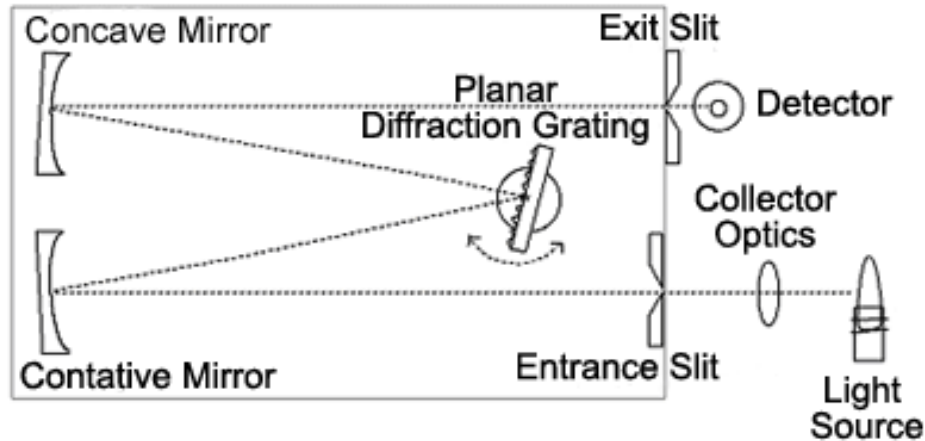
$$I = F_{\text{c}} \frac{h \times c \times g_m \times A \times N}{4\pi \times l \times Z} \times \exp\left(-\frac{E_m}{kT}\right)$$

- intensity of a spectral line  $\sim N$ , i.e.  $\sim C$
- population of excited states requires high temperatures (typical 2000 K-7000 K)
- relative method, calibration required



$$I = \frac{h \times c}{E}$$

### 2.3.1 Atomic Emission Spectroscopy

#### instrumentation



#### radiation sources (classification)

inductively coupled plasma (ICP)	liquid samples	
flame		
spark	solid samples	
arc		
glow discharge		
laser		

#### analytical performance

- multielement method (with arc 60-70 elements)
- precision:  $\pm 1\%$  RSD for spark, flame and plasma; arc 5-10% RSD
- decision limits: 0.1-1 ppm with arc, 1-10ppm with spark, 1ppb-10ppm with flame, 10ppt-5ppb for ICP

#### application:

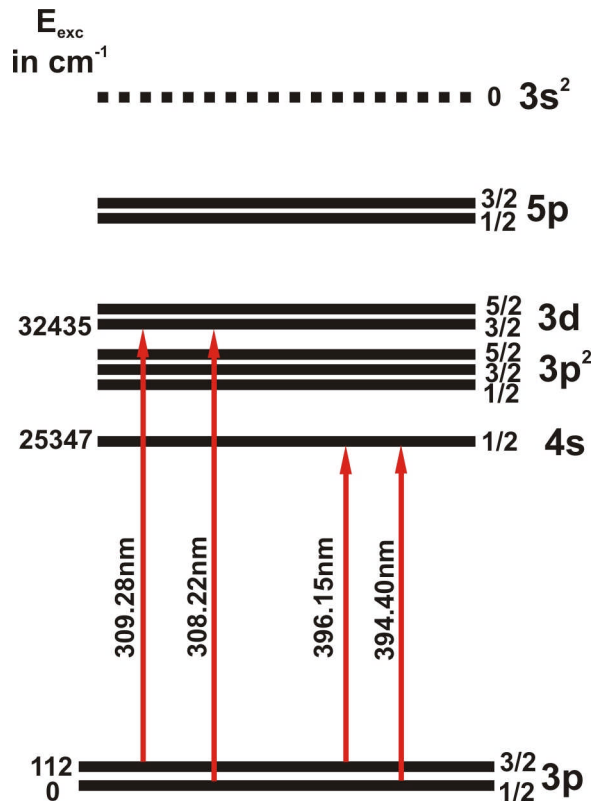
- flame AES – low cost system for alkali and earth alkaline metals
- ICP AES – suited for any sample that can be brought into solution
- arc AES – with photographic plate for qualitative overview analysis
- spark AES – unsurpassable for metal analysis (steel, alloys)
- laser ablation – for direct analysis of solids (transient signals)

## 2.3 Spectroscopic Methods

### 2.3.2 Atomic Absorption Spectroscopy

- principle: measurement of the absorption of light by free atoms in their electronic ground state

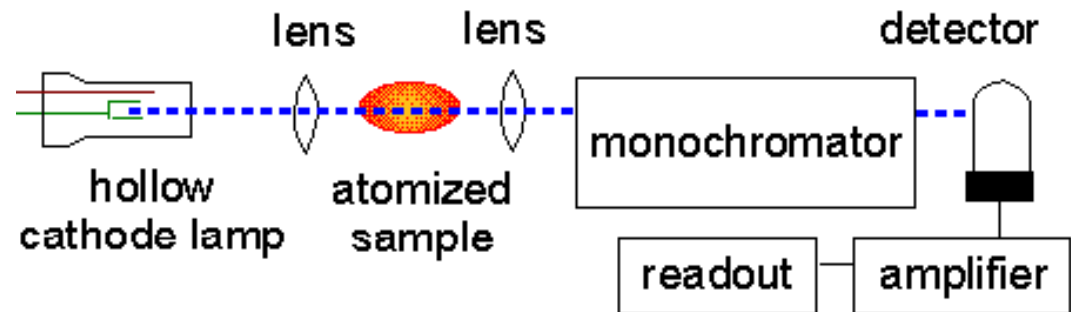
#### ground and excited states of Al and optical transitions used for AAS



#### linear relation between absorbance and concentration

$$A_{abs} = \log \frac{I_0}{I} = 0.434 \times A \times \frac{g_m}{g_0} \times \frac{1}{8\pi c} \times \frac{1}{Dl_{eff}} \times n_0 \times l$$

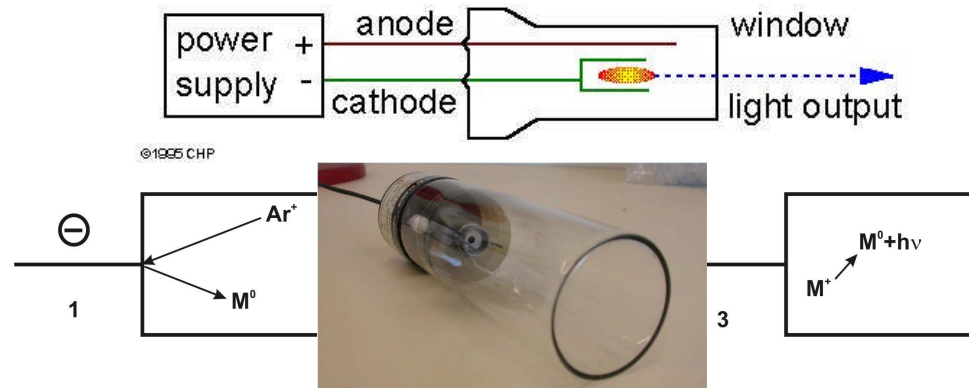
#### AAS instrumentation



#### radiation source

- atomic absorption lines are very small ( $\Delta \lambda \approx 0.005 \text{ nm}$ )  $\Rightarrow$  narrow excitation lines required
- hollow cathode lamp filled with Ar ( $\sim 5 \text{ Torr}$ )  $\Rightarrow$  discharge in cathode cup
- cup-shaped cathode made from the element to be determined  $\Rightarrow$  emission of sharp de-excitation lines

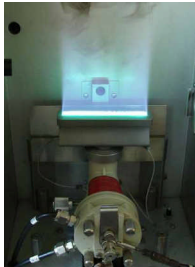
#### working principle of hollow cathode lamps



#### source of free atoms

##### flame

- pneumatic nebulization of the liquid sample into the flame or hydride generation (e.g. for As, Bi, Ge)
- air/ $\text{C}_2\text{H}_2$  for nonrefractory elements (e.g. Ca, Cr, Fe)
- $\text{N}_2\text{O}/\text{C}_2\text{H}_2$  for refractory elements (e.g. Al, Si, Ta)



##### graphite furnace

- electrically heated graphite tube ( $T_{\text{max}} = 3000^\circ\text{C}$ , under Ar)
- T vs. t program  $\Rightarrow$  drying, ashing, atomization, cleaning
- transient signals
- liquid and solid samples

### 2.3.2 Atomic Absorption Spectroscopy

#### interferences in atomic absorption spectroscopy

- flame and furnace AAS are sensitive to matrix interferences ⊃ i.e. matrix constituents (anything but the analyte) influence the analyte signal
- there are two types of interferences ⊃ chemical and spectral interferences

#### chemical interferences

- limited temperature of the flame does not ensure full dissociation and atomization of thermally stable compounds (e.g. Ca phosphates) ⊃ hotter N<sub>2</sub>O flame (La buffer)
- large amounts of easily ionized elements (alkali metals) modifies the equilibrium between atoms and ions ⊃ adding excess of Cs
- loss of volatile analyte species during the ashing process in GF-AAS (e.g. ZnCl<sub>2</sub>) ⊃ adding of matrix modifiers



#### spectral interferences

- two spectral lines overlap within the band pass of the dispersive element (e.g.  $\Delta \lambda_d \gg 0.1\text{nm}$ , Cd 228.802nm and As 228.812nm) ⊃ select another line
- nonspecific absorptions from solid or liquid particles in the atomizer (e.g. light scattering by liquid or solid NaCl particles)
- emission of molecular bands by molecules and radicals present in the atomizer (metal halides from 200 - 400nm)
- background correction necessary



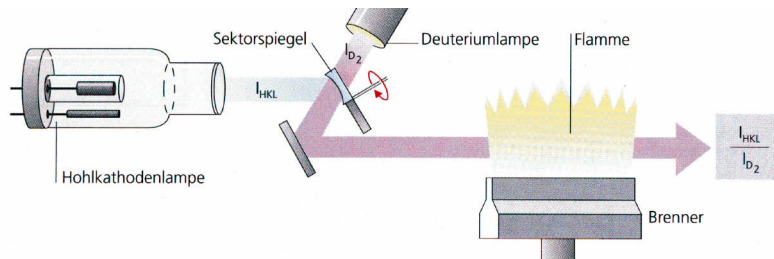
## 2.3 Spectroscopic Methods

### 2.3.2 Atomic Absorption Spectroscopy

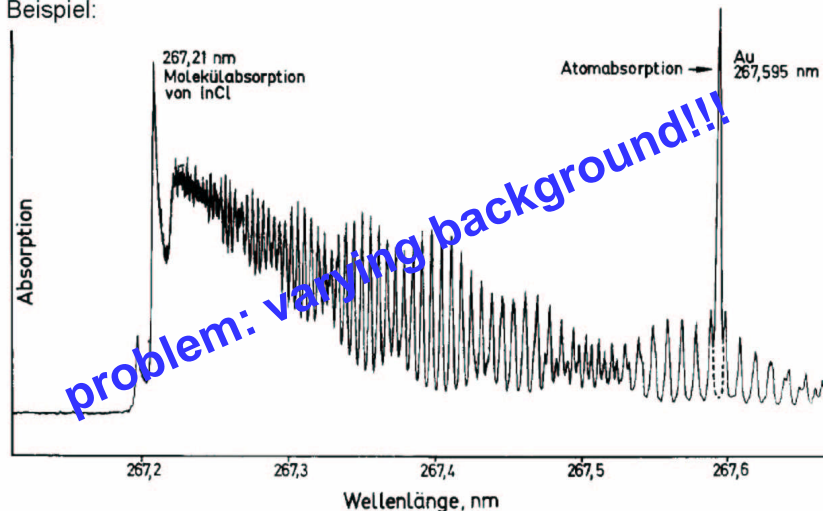
#### deuterium background correction

- deuterium lamp emits a continuous spectrum in the range 200-380nm
- alternating measurement of deuterium and hollow cathode lamp absorption

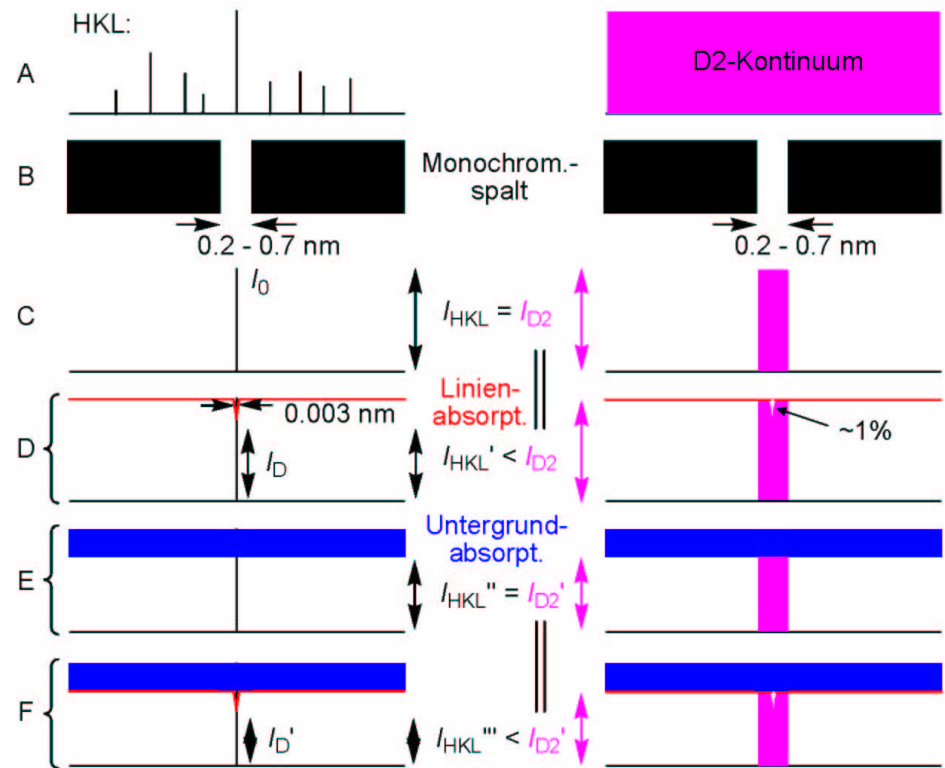
#### setup sketch



Beispiel:



#### working principle





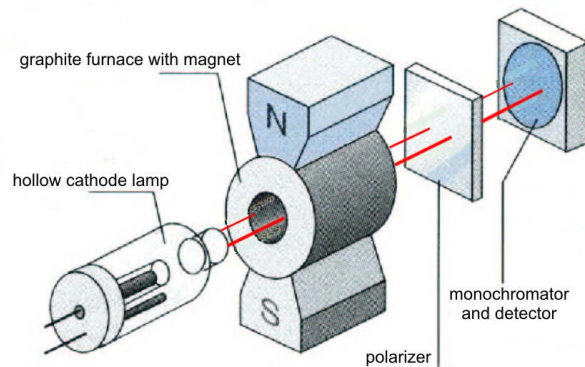
## 2.3 Spectroscopic Methods

### 2.3.2 Atomic Absorption Spectroscopy

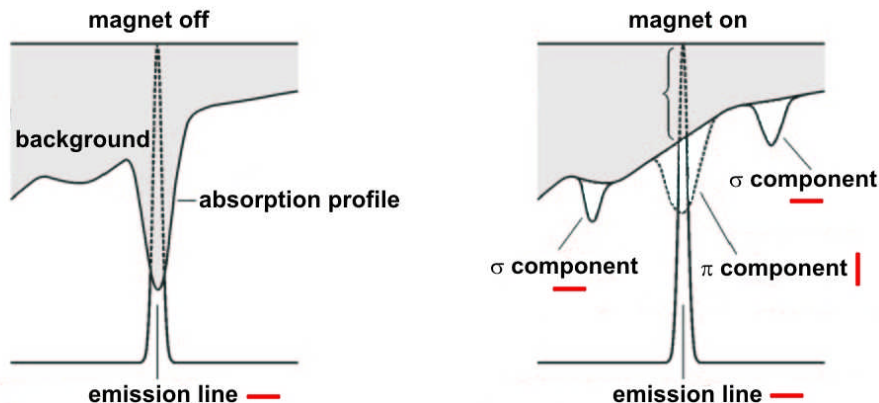
#### Zeeman background correction

- Zeeman effect: splitting of atomic energy levels in a magnetic field
- applied in AAS for correction of strong varying backgrounds

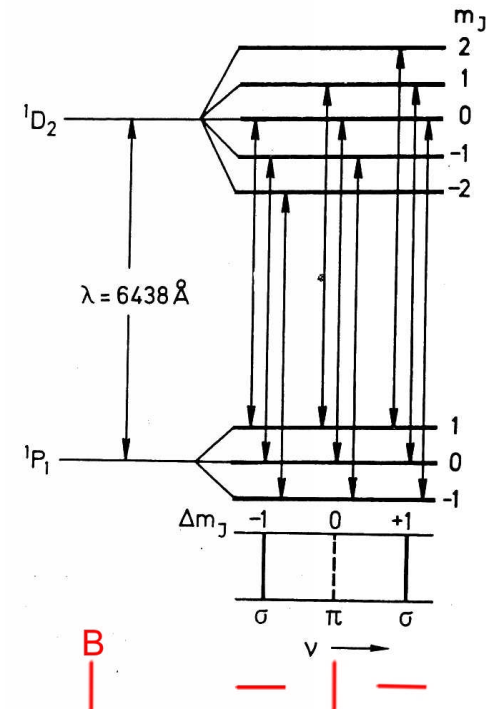
#### setup sketch



#### working principle



#### normal Zeeman effect (S=0) (e.g. Cd atoms)



## 2.3 Spectroscopic Methods

### 2.3.2 Atomic Absorption Spectroscopy

#### analytical performance

➤ AAS is most popular among the instrumental methods for elemental analysis

#### flame-AAS:

- relatively good limits decision limits (ng/ml)
- working range mg/l (liner range)
- easy to use, stable, comparably cheap
- few and well known spectral interferences
- single element method (up to 6 in parallel)
- high sample consumption

#### graphite furnace – AAS:

- superior decision limits (pg/ml) (trace and ultra-trace analysis)
- very low sample consumption
- analysis of solids and liquids
- analyte matrix separation possible
- demanding operation

PERKIN ELMER

Elemental Analysis Table showing recommended flame types and wavelengths for various elements.

Legend:

- Elemental Analysis Table
- Recommended Flame Type
- Recommended Wavelength (nm)
- Recommended Wavelength (nm)

Elements listed include: H, He, Li, Be, Na, Mg, K, Ca, Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Ga, Ge, As, Se, Br, Kr, Rb, Sr, Y, Zr, Nb, Mo, Tc, Ru, Rh, Pd, Ag, Cd, In, Sn, Sb, Te, I, Xe, Cs, Ba, La, Hf, Ta, W, Re, Os, Ir, Pt, Au, Hg, Tl, Pb, Bi, Po, At, Rn, Fr, Ra, Ac.

Nachweisgrenzen (ng/mL)

Legend:

- ICP-Emission
- Flammenatomabsorption
- Graphitrohr-Atomabsorption

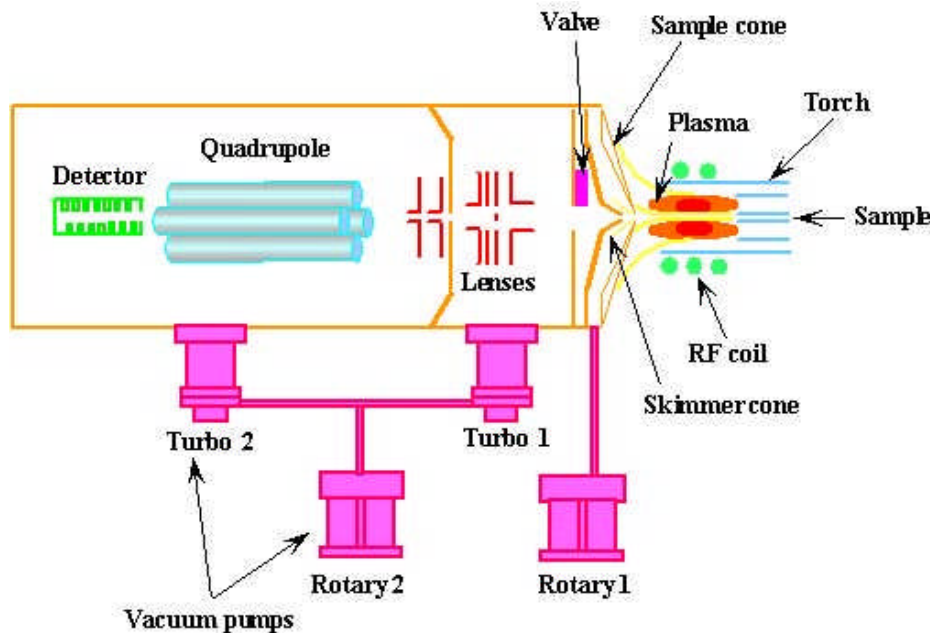
Table showing detection limits for various elements using different methods.

Elements listed include: Li, Be, Na, Mg, K, Ca, Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Ga, Ge, As, Se, Br, Kr, Rb, Sr, Y, Zr, Nb, Mo, Tc, Ru, Rh, Pd, Ag, Cd, In, Sn, Sb, Te, I, Xe, Cs, Ba, La, Hf, Ta, W, Re, Os, Ir, Pt, Au, Hg, Tl, Pb, Bi, Po, At, Rn, Th, Pa, U, Np, Pu, Am, Cm, Bk, Cf, Es, Fm, Md, No, Lr.

### 2.3.3 Inductively Coupled Plasma Mass Spectrometry

- a mass spectrometer separates a stream of gaseous ions into ions with different mass to charge ratio  $m/z$  (mass range in inorganic mass spectrometry from 1 – 300 u)
- in combination with an ion source (ICP, spark, glow discharge, laser ablation) as analytical method for elemental analysis
- most popular combination  $\supset$  Inductively Coupled Plasma + quadrupole Mass Spectrometer = ICP - MS

#### setup scheme



#### sample introduction

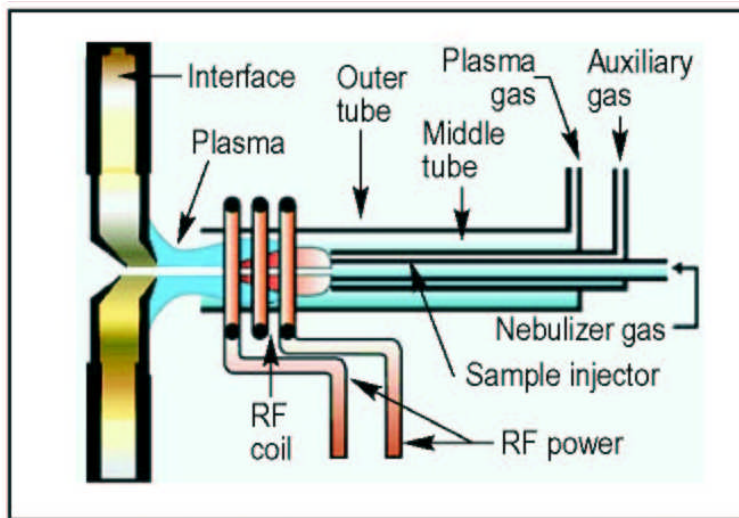
- pneumatic nebulizer  
(liquid samples)
- electro thermal vaporization  
(graphite furnace)  
liquid and solid samples
- laser ablation  
solid samples

## 2.3.3 Inductively Coupled Plasma Mass Spectrometry

## ICP as ion source

- plasma generation by inductively heating of a gas (e.g. argon) using a high frequency field

## ICP assembly

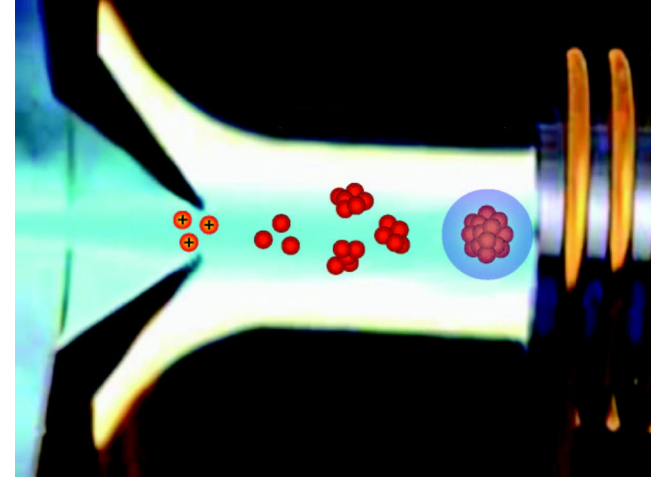


- ICP works under atmospheric pressure, MS under high vacuum ▸ differentially pumped interface required
- typical RF frequencies 27 or 40 MHz
- power consumption 1 – 5 kW



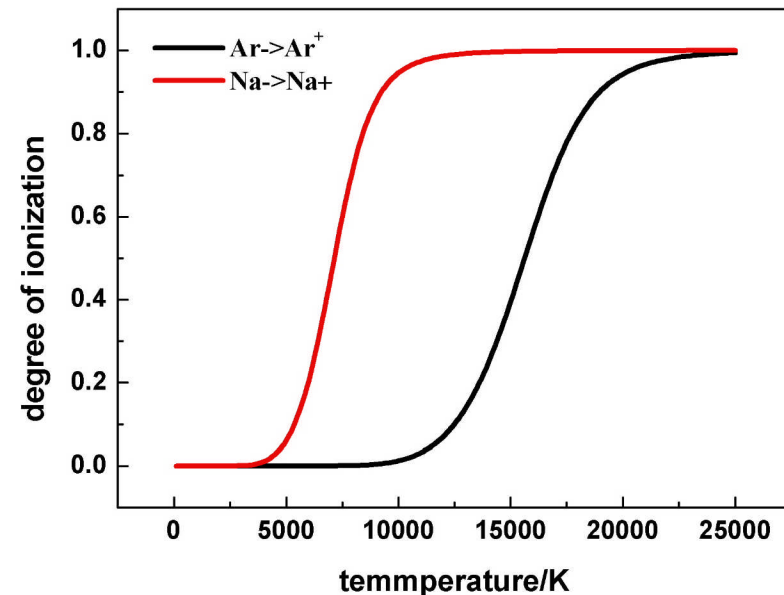
### 2.3.3 Inductively Coupled Plasma Mass Spectrometry

- sample droplets + carrier gas (inner tube connected to nebulizer) punch a channel through the toroidal plasma
- sample transformations in the plasma:  
desolvation ® vaporization ® atomization ® ionization
- ionization behavior depends on the temperature  $\triangleright$  Saha equation (law of mass action for ionization equilibria)



$$\frac{a_i(1 + a_e)}{a_{i+1}a_e} = pK_p^{(i+1)}(T) \quad K_p^{(i+1)}(T) = \frac{g_i}{g_e g_{i+1}} \frac{1}{T} \exp\left(-\frac{I_{i+1}}{RT}\right)$$

- example:  $\text{Ar}^0(1S_0) \rightleftharpoons \text{Ar}^+(2P_{3/2})$   $I_+ = 15.76 \text{ eV}$ , 1 bar  
 $\text{Na}^0(2S_{1/2}) \rightleftharpoons \text{Na}^+(1S_0)$   $I_+ = 5.14 \text{ eV}$





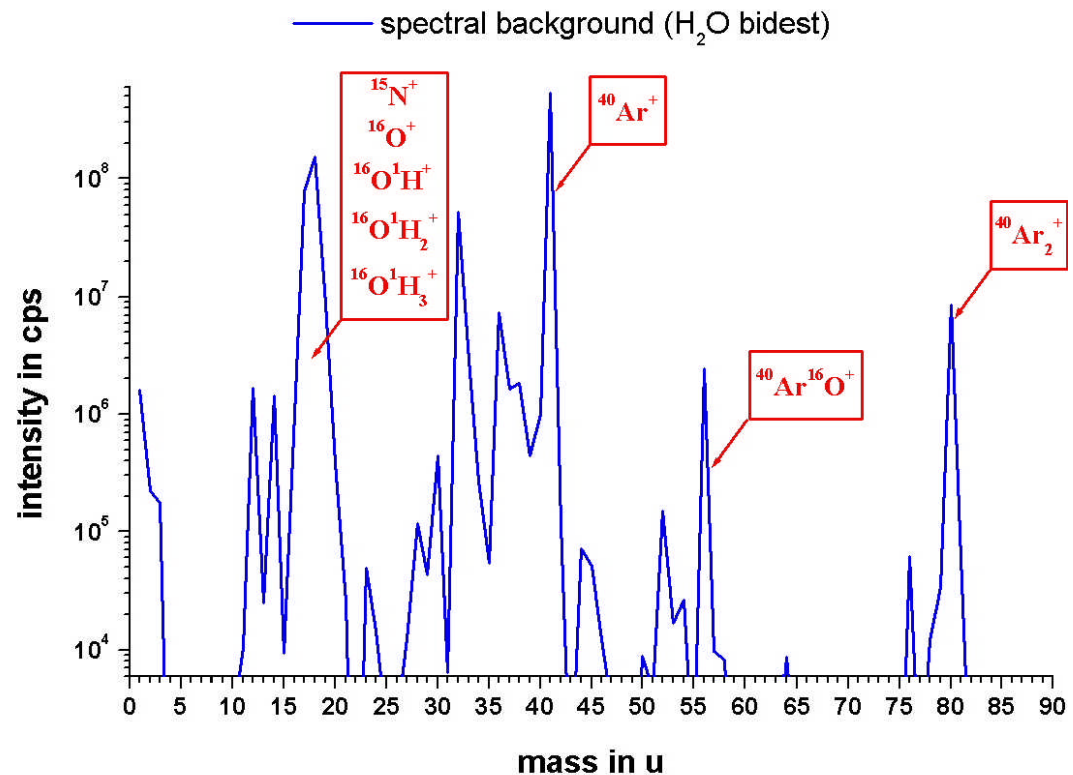
### 2.3.3 Inductively Coupled Plasma Mass Spectrometry

- determination of elements  $Z < 80$  u by ICP - MS suffers from spectral interferences caused by the plasma gas, solvent, sample matrix etc.

#### types of spectral interferences

- isobaric overlaps
- oxide-, hydroxide species
- doubly charged ions

interference	analyte
$^{40}\text{Ar}^+$	$^{40}\text{Ca}^+$
$^{40}\text{Ar}^{16}\text{O}^+$	$^{56}\text{Fe}^+$
$^{138}\text{Ba}^{2+}$	$^{69}\text{Ga}^+$

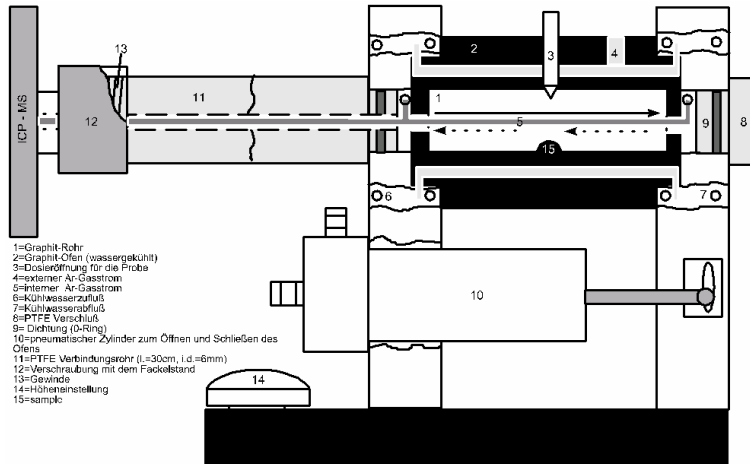
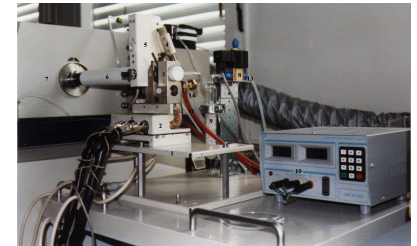
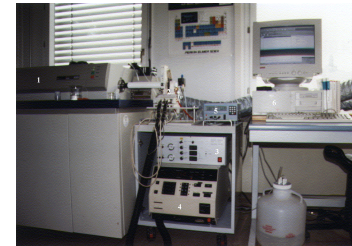


- spectral interferences cause a high background  $\supset$  higher decision limit for disturbed analytes (e.g.  $x_d(\text{Fe}) \gg 10 \mu\text{g/l}$ ,  $x_d(\text{Ag}) \gg 0.03 \mu\text{g/l}$ )

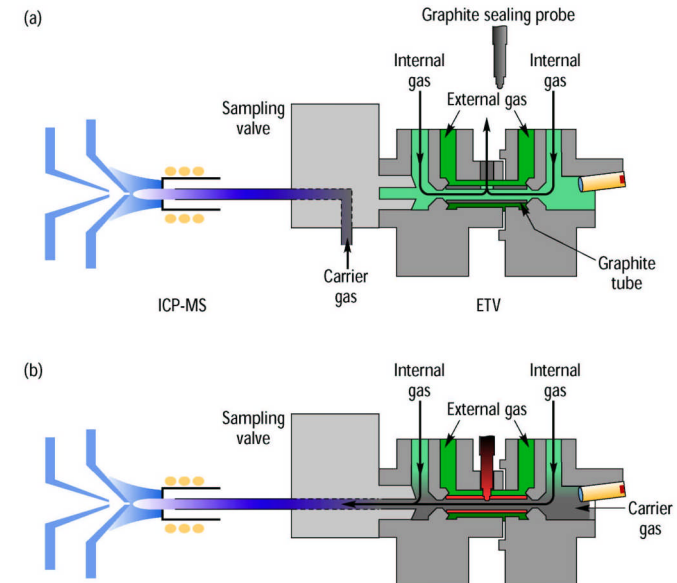
- analyte – matrix separation by coupling of an **ElectroThermal Vaporization** to the **ICP-MS** ® **ETV-ICP-MS**

setup picture

scheme of the ETV unit



operation principle



- quenching of the sample vapor by mixing it with cold carrier gas

$$d_k = 4S \times \frac{V_m}{k \times T \times \ln S} \quad S = \frac{p}{p_{eq}(T)}$$

- sample transport as condensed particles if the condensation nuclei exceed the critical diameter

- one touchstone in ICP-MS analytics is the determination of light elements in saline solutions, e.g. seawater)
- example: Zn determination in sea water



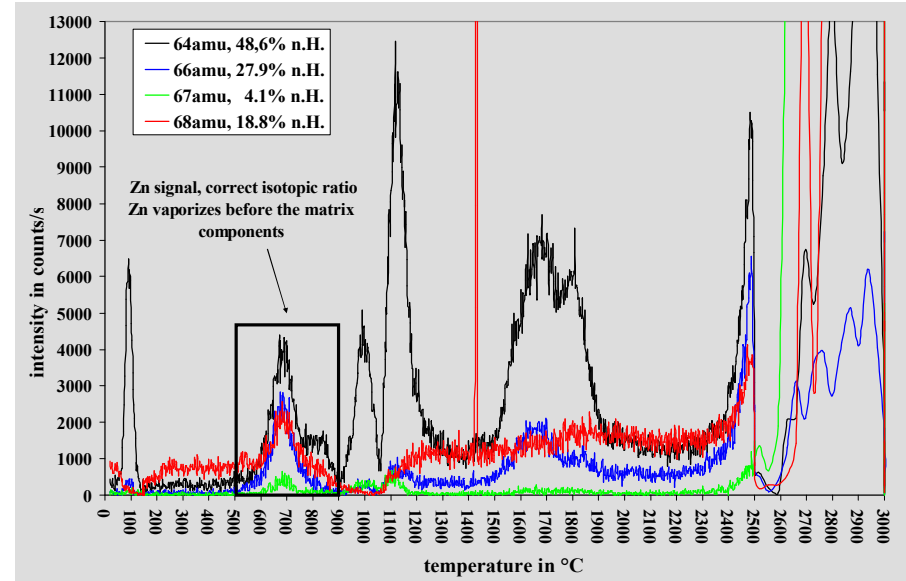
### relevant spectral interferences

ion	64 u	66 u	67 u	68 u	concentration in seawater
$\text{Zn}^{2+}$	48.6% n.a.	27.9% n.a.	4.1% n.a.	18.8% n.a.	~1 ng/ml
$\text{Cl}^-$			$^{35}\text{Cl}^{16}\text{O}^{16}\text{O}^+$	$^{35}\text{Cl}^{16}\text{O}^{17}\text{O}^+$	ca. 16 mg/l
$\text{SO}_4^{2-}$	$^{32}\text{S}^{16}\text{O}^{16}\text{O}^+$ $^{32}\text{S}^{32}\text{S}^+$	$^{34}\text{S}^{16}\text{O}^{16}\text{O}^+$ $^{32}\text{S}^{34}\text{S}^+$ $^{33}\text{S}^{33}\text{S}^+$ $^{32}\text{S}^{17}\text{O}^{17}\text{O}^+$ $^{32}\text{S}^{16}\text{O}^{18}\text{O}^+$ $^{33}\text{S}^{16}\text{O}^{17}\text{O}^+$	$^{33}\text{S}^{34}\text{S}^+$ $^{32}\text{S}^{17}\text{O}^{18}\text{O}^+$ $^{33}\text{S}^{16}\text{O}^{18}\text{O}^+$ $^{33}\text{S}^{17}\text{O}^{17}\text{O}^+$ $^{34}\text{S}^{16}\text{O}^{17}\text{O}^+$	$^{36}\text{S}^{16}\text{O}^{16}\text{O}^+$ $^{32}\text{S}^{36}\text{S}^+$ $^{34}\text{S}^{17}\text{O}^{17}\text{O}^+$ $^{34}\text{S}^{16}\text{O}^{18}\text{O}^+$ $^{34}\text{S}^{34}\text{S}^+$ $^{33}\text{S}^{17}\text{O}^{18}\text{O}^+$ $^{32}\text{S}^{18}\text{O}^{18}\text{O}^+$	ca. 2 mg/l
$\text{Mg}^{2+}$	$^{24}\text{Mg}^{40}\text{Ar}^+$ $^{26}\text{Mg}^{38}\text{Ar}^+$	$^{26}\text{Mg}^{40}\text{Ar}^+$			ca. 1 mg/ml

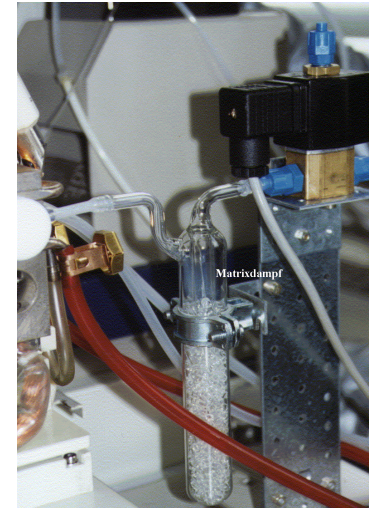


### application to the Zn in seawater problem

- analyte – matrix separation by ETV
- sample matrix can be vaporized prior the analyte or in reversed fashion
- application of modifiers (ETV as thermochemical reactor, cp. atomic absorption spectroscopy)
- resulting temperature – time program

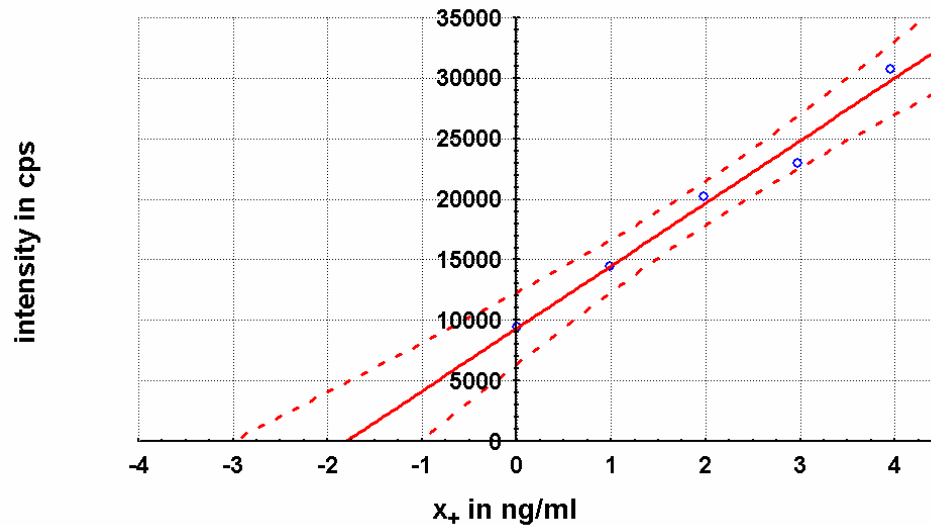


step	T / °C	ramp time / s	hold time / s	function
1	150	10	60	drying
2	150	0	30	baseline
3	800	1	59	Zn vaporization (prob. as $\text{ZnCl}_2$ BP=732°C)
4	2500	5	5	cleaning



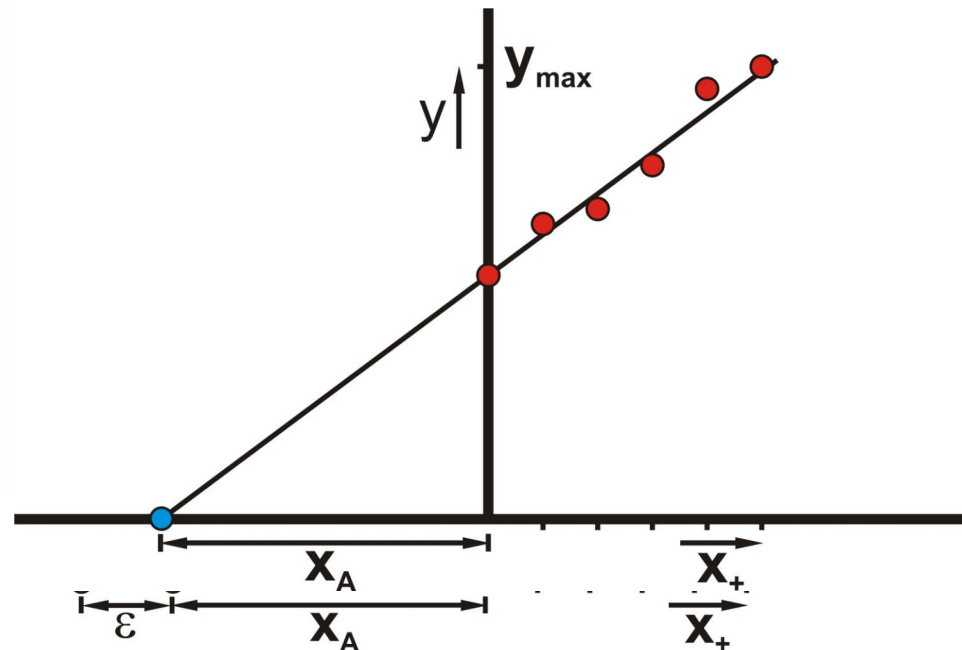
- if matrix matched calibration samples are not available  $\supset$  standard addition
- principle of the standard addition method:
  - measurement of the analysis sample
  - stepwise addition of analyte ( $x_+ = x_A \dots 4x_A$ )
  - evaluation of  $x_A$  by extrapolation of the calibration function to the intercept point with the x-axis ( $y = f(x_+) = 0 \supset x_A$ )

Zn in seawater by ETV-ICP-MS  
standard addition



result:  $1 \text{ ng/ml} < C_{\text{Zn}} < 3 \text{ ng/ml}$

certified value: 1.24 ng/ml



#### analytical performance of ICP-MS

- multi-element method (more than 20 analytes in parallel)
- good performance in precision (a few percent), accuracy, number of determinable elements, decision limit (depending on the instrument 0.01-100 ng/l) and sample throughput
- linear dynamic range  $\supset$  3-5 orders of magnitude
- difficult for elements with  $m/z < 80$  u (spectral interferences)
- mostly applied for liquid sample, ETV and laser vaporization enable direct analysis of solid samples
- supplies information about the isotopic ratio of an element
  - isotope dilution analysis for ultra-trace analysis (sub ppt range)
  - age determination of biological and geological samples
- relatively young analysis method (1980)  $\supset$  high innovative potential



## Specificity and Selectivity of Analytical Methods

### specificity...

- ...describes the ability of a method to detect 1 particular analyte on 1 sensor undisturbed from all other components present in the sample
- ...refers to a single component analysis
- ...is based upon the concept of partial sensitivities  $S_{IJ} = \frac{\partial y_I}{\partial x_J}$

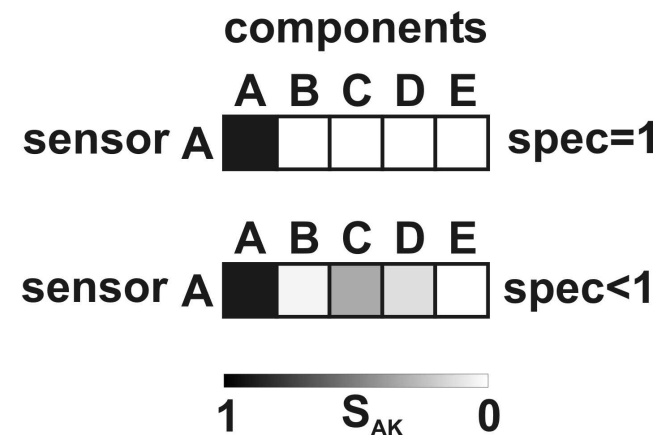
vector of partial sensitivities

$$\underline{s}_A = (S_{AA} S_{AB} \dots S_{AZ})$$

$$spec(A/B, \dots, Z) = \frac{S_{AA} \times x_A}{\sum_{K=A}^Z S_{AK} \times x_K}$$

$$0 \leq spec(A/B, \dots, Z) \leq 1$$

for practical work  $spec(A/B, \dots, Z) > 0.9$  sufficient



### selectivity...

- ...describes the ability of a method to determine  $n$  analytes on  $n$  sensors undisturbed and independent from each other and from other components present in the sample
- ...refers to a multi-component analysis
- ...is based upon the concept of partial sensitivities

$$S_{IJ} = \frac{\partial y_I}{\partial x_J}$$

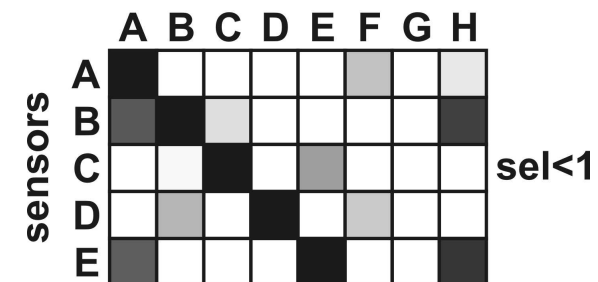
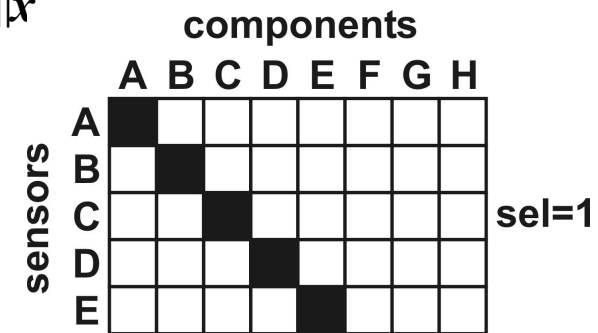
matrix of partial sensitivities

$$\underline{S} = \begin{pmatrix} S_{AA} & S_{AB} & \cdots & S_{AN} & S_{AN+1} & \cdots & S_{AZ} \\ S_{BA} & S_{BB} & \cdots & S_{BN} & S_{BN+1} & \cdots & S_{BZ} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \cdots & \vdots \\ S_{NA} & S_{NB} & \cdots & S_{NN} & S_{NN+1} & \cdots & S_{NZ} \end{pmatrix}$$

$$\text{sel}(A, B, \dots, N / N + 1, \dots, Z) = \frac{\sum_{I=A}^N \sum_{J=A}^Z S_{IJ} \times x_I}{\sum_{I=A}^N \sum_{J=A}^Z S_{IJ} \times x_I}$$

$$0 \leq \text{sel}(A, B, \dots, N / N + 1, \dots, Z) \leq 1$$

for practical work  $\text{sel}(A, B, \dots, N / N + 1, \dots, Z) > 0.9$  sufficient



- application of the selectivity/specificity concept to compare PN-ICP-MS and ETV-ICP-MS for the determination of Zn in seawater

**specificity matrix for the sensors (masses) 64,66,67,68 u**

$$S = \begin{pmatrix} \frac{\Delta I_{64\text{amu}}}{\Delta C_{\text{Zn}^{2+}}} & \frac{\Delta I_{66\text{amu}}}{\Delta C_{\text{Zn}^{2+}}} & \frac{\Delta I_{67\text{amu}}}{\Delta C_{\text{Zn}^{2+}}} & \frac{\Delta I_{68\text{amu}}}{\Delta C_{\text{Zn}^{2+}}} \\ \frac{\Delta I_{64\text{amu}}}{\Delta C_{\text{Cl}^-}} & \frac{\Delta I_{66\text{amu}}}{\Delta C_{\text{Cl}^-}} & \frac{\Delta I_{67\text{amu}}}{\Delta C_{\text{Cl}^-}} & \frac{\Delta I_{68\text{amu}}}{\Delta C_{\text{Cl}^-}} \\ \frac{\Delta I_{64\text{amu}}}{\Delta C_{\text{SO}_4^{2-}}} & \frac{\Delta I_{66\text{amu}}}{\Delta C_{\text{SO}_4^{2-}}} & \frac{\Delta I_{67\text{amu}}}{\Delta C_{\text{SO}_4^{2-}}} & \frac{\Delta I_{68\text{amu}}}{\Delta C_{\text{SO}_4^{2-}}} \\ \frac{\Delta I_{64\text{amu}}}{\Delta C_{\text{Mg}^{2+}}} & \frac{\Delta I_{66\text{amu}}}{\Delta C_{\text{Mg}^{2+}}} & \frac{\Delta I_{67\text{amu}}}{\Delta C_{\text{Mg}^{2+}}} & \frac{\Delta I_{68\text{amu}}}{\Delta C_{\text{Mg}^{2+}}} \end{pmatrix}$$

**test samples to determine S**

sample	[Zn <sup>2+</sup> ] in ng/ml	[Cl <sup>-</sup> ] in mg/ml	[SO <sub>4</sub> <sup>2-</sup> ] in mg/ml	[Mg <sup>2+</sup> ] in mg/ml
1	50	10	1	0.5
2	100	10	1	0.5
3	50	20	1	0.5
4	50	10	5	0.5
5	50	10	1	1.5

### ➤ experimental specificity matrices after t-test (comparison of two mean values)

$$S_{PN} = \begin{matrix} & \begin{matrix} 64amu & 66amu & 67amu & 68amu \end{matrix} \\ \begin{matrix} Zn^{2+} \\ Cl^- \\ SO_4^{2-} \\ Mg^{2+} \end{matrix} & \begin{matrix} 616 & 378 & 63.9 & 265 \\ 1.22 \cdot 10^{-3} & -3.48 \cdot 10^{-4} & 0 & 0 \\ 18.6 \cdot 10^{-3} & 0 & 0 & 0 \\ 28.5 \cdot 10^{-3} & 14.3 \cdot 10^{-3} & 2.52 \cdot 10^{-3} & 8.97 \cdot 10^{-3} \end{matrix} \end{matrix}$$

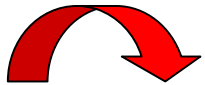
$$S_{ETV} = \begin{matrix} & \begin{matrix} 64amu & 66amu & 67amu & 68amu \end{matrix} \\ \begin{matrix} Zn^{2+} \\ Cl^- \\ SO_4^{2-} \\ Mg^{2+} \end{matrix} & \begin{matrix} 5669 & 3557 & 524 & 2438 \\ -10.2 \cdot 10^{-3} & -5.67 \cdot 10^{-3} & -1.01 \cdot 10^{-3} & -4.13 \cdot 10^{-3} \\ 0 & -23.0 \cdot 10^{-3} & 0 & -17.3 \cdot 10^{-3} \\ 0 & -40.4 \cdot 10^{-3} & 0 & -33.4 \cdot 10^{-3} \end{matrix} \end{matrix}$$

- ETV-ICP-MS about 10 times more sensitive than PN-ICP-MS
- positive partial sensitivities in  $S_{PN}$  reflect spectral interferences (e.g. interference of  $^{24}Mg^{40}Ar^+$  and  $^{26}Mg^{38}Ar^+$  on  $^{64}Zn^+$ )
- negative partial sensitivities in  $S_{ETV}$  reflect non-spectral interferences
- influence of  $Cl^-$ :  $Zn^{2+} + 2Cl^- \rightleftharpoons ZnCl_{2(s)} \rightleftharpoons ZnCl_{2(g)}$   
(the less  $Cl^-$  in solution the less  $Zn^{2+}$  vaporizes as  $ZnCl_2$ )  $\supset$  non-spectral interference due to sample transport mechanism
- influence of  $SO_4^{2-}$  on the drying step:  $Zn^{2+} + SO_4^{2-} \rightleftharpoons ZnSO_{4(s)}$   
above  $770^\circ C$   $ZnSO_{4(s)} \rightleftharpoons ZnO$  (mp =  $1974^\circ C$ ) +  $SO_2 + \frac{1}{2} O_2$   
 $\supset$  as the vaporization step is done at  $800^\circ C$   $SO_4^{2-}$  ions cause a loss of  $Zn^{2+}$



➤ specificities for a typical seawater sample

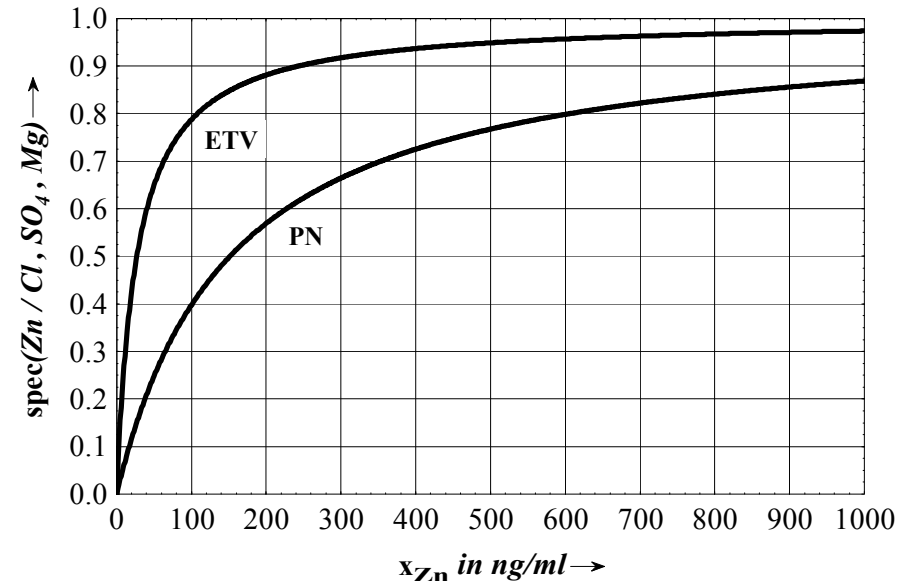
ion	C in ng/ml	S <sub>prakt.</sub> 64amu PN	S <sub>prakt.</sub> 66amu PN	S <sub>prakt.</sub> 67amu PN	S <sub>prakt.</sub> 68amu PN	S <sub>prakt.</sub> 64amu ETV	S <sub>prakt.</sub> 66amu ETV	S <sub>prakt.</sub> 67amu ETV	S <sub>prakt.</sub> 68amu ETV
Zn <sup>2+</sup>	75	0.33	0.59	0.66	0.69	0.74	0.59	0.72	0.57
Cl <sup>-</sup>	15×10 <sup>6</sup>								
SO <sub>4</sub> <sup>2-</sup>	2.5×10 <sup>6</sup>								
Mg <sup>2+</sup>	1.0×10 <sup>6</sup>								



no external calibration  
(i.e. standards) possible  
for ng/ml concentrations

$$spec_{PN,64amu}(Zn^{2+} / Cl^{-}, SO_4^{2-}, Mg^{2+}) = \frac{616 \times x_{Zn^{2+}}}{616 \times x_{Zn^{2+}} + 93300}$$

$$spec_{ETV,64amu}(Zn^{2+} / Cl^{-}, SO_4^{2-}, Mg^{2+}) = \frac{5669 \times x_{Zn^{2+}}}{5669 \times x_{Zn^{2+}} + 153000}$$

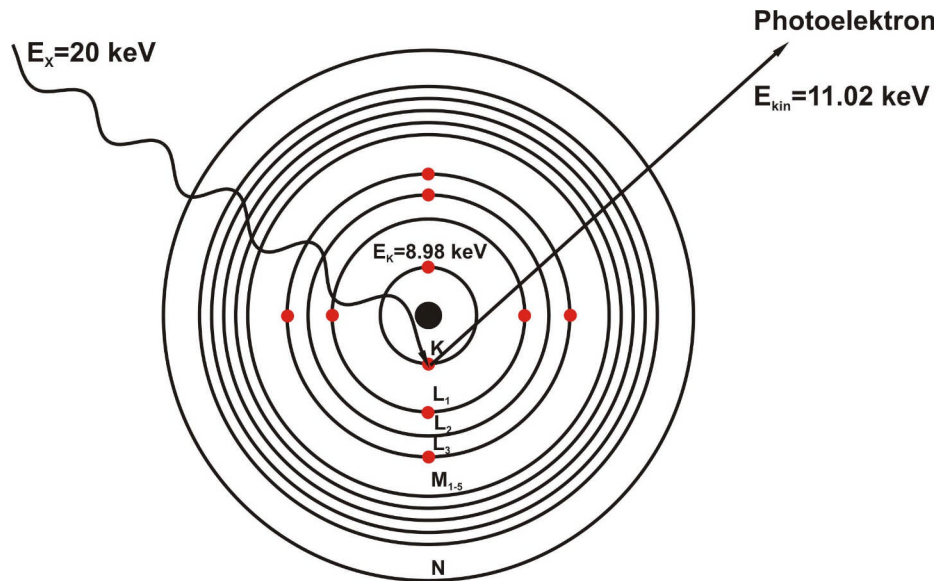


## 2.3 Spectroscopic Methods

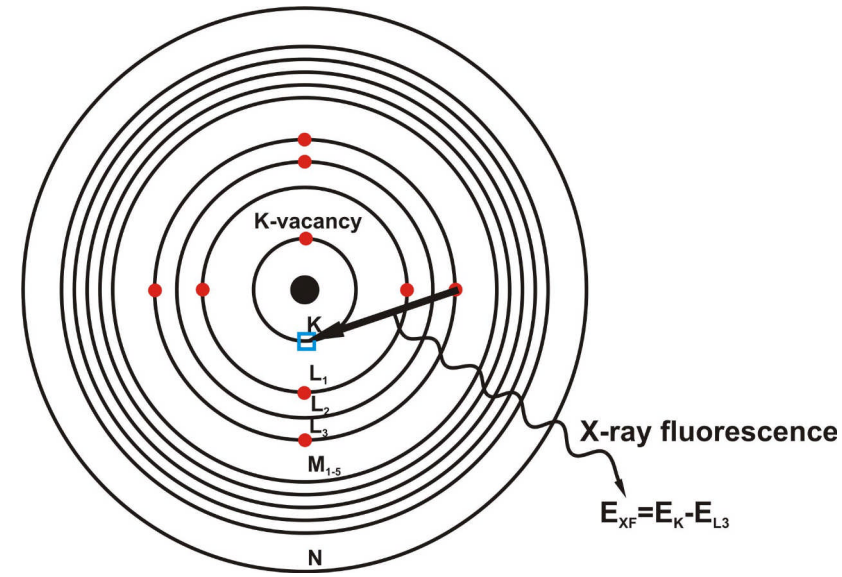
### 2.3.4 X-Ray Fluorescence Spectroscopy

- instrumental analytical technique for the elemental analysis of solids and liquids
- wide concentration ranges (ppm - %), minimal sample preparation
- principle: detection of element specific X – rays (characteristic X-rays) emitted from a sample under X-ray excitation (X-ray fluorescence)

#### interaction of X-rays with matter



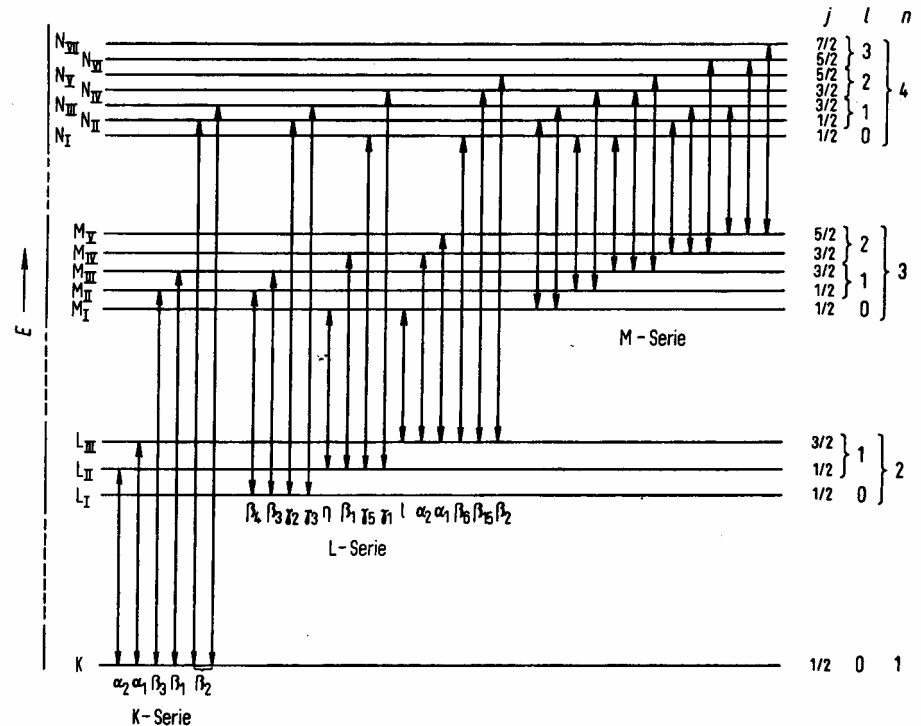
emission of a core level electron (here from copper) by absorption of a X-ray photon



energetic relaxation by X-ray fluorescence

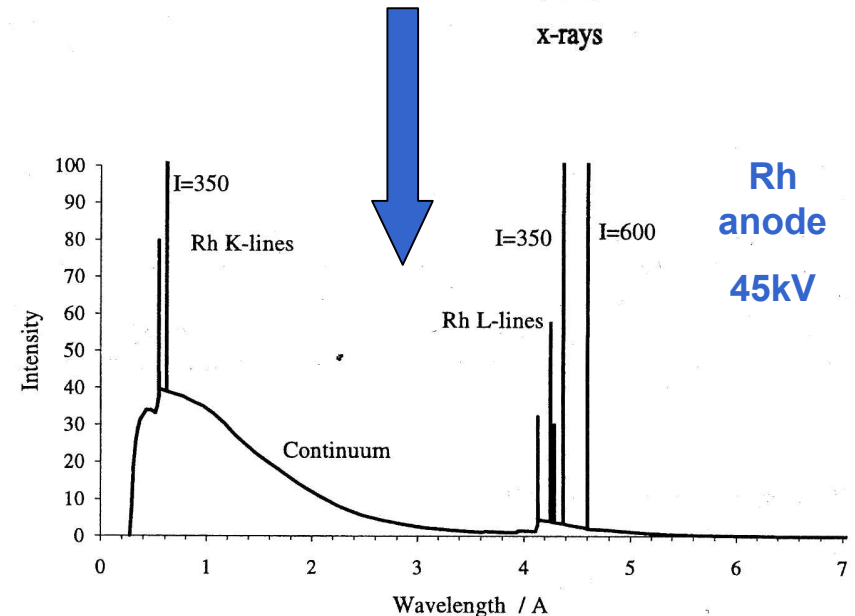
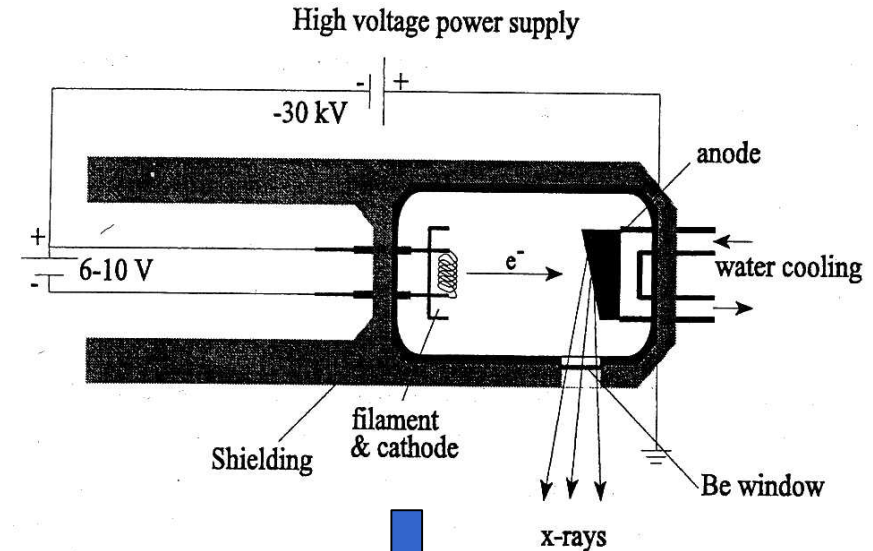
- transitions are governed by quantum mechanical selection rules ( $\Delta n > 1$ ,  $\Delta l = \pm 1$ ,  $\Delta j = 0, \pm 1$ )
- K – lines originate from vacancies in the K – shell, L – lines from vacancies in the L – shell ...
- denotation of lines:
  - i) IUPAC notation – Fe  $KL_3$
  - ii) Siegbahn notation – Fe  $a_1$
- line intensities depend on:
  - i) the energetic difference of the levels (the higher the energetic difference the lower the transition probability)
  - ii) the degeneracy of the levels
  - iii) the fluorescence yield
- K – lines best suited for analysis of elements  $Z < 45$  (Rh) (mostly K- $L_{3,2}$ )
- L – lines for analysis of elements  $Z > 45$  (mostly  $L_3$ - $M_{5,4}$ )

### atomic energy levels and allowed transitions



#### instrumentation – X-ray source

- generation of X-rays by collision of high energetic electrons with a pure metal target (Rh, Mo, Cr, Ag, W)
- continuous X-rays by decelerating collisions with the target atoms (Bremsstrahlung)
- characteristic X-rays by refilling of core level vacancies in the target atoms created by the impinging electrons
- the short wavelength limit of the source depends on the accelerating voltage, the long wavelength tail depends on the Be-window thickness
- only ~1% of the electric power is converted to X-rays, rest is heat ⊃ effective water or air cooling required
- quantitative work ⊃ stable filament heating and accelerating voltage required

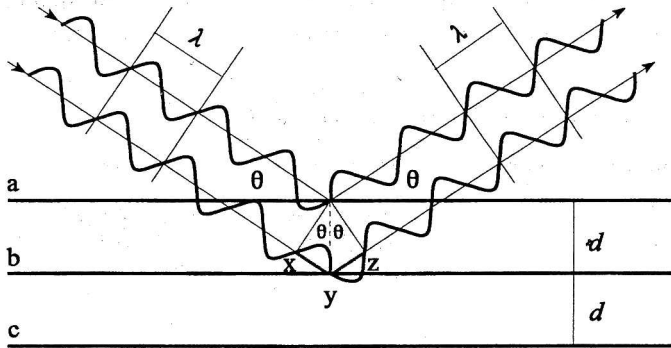


## 2.3 Spectroscopic Methods

### 2.3.4 X-Ray Fluorescence Spectroscopy

#### instrumentation – wavelength dispersive instruments

- irradiated sample emits polychromatic X-rays

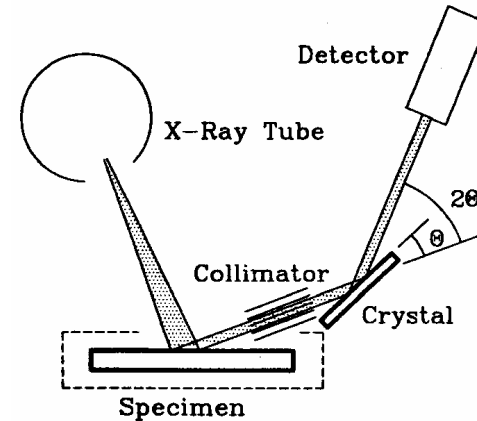


- crystal as dispersive element
- wavelength selection according to Bragg's law

$$n \times \lambda = 2 \times d \times \sin \theta$$

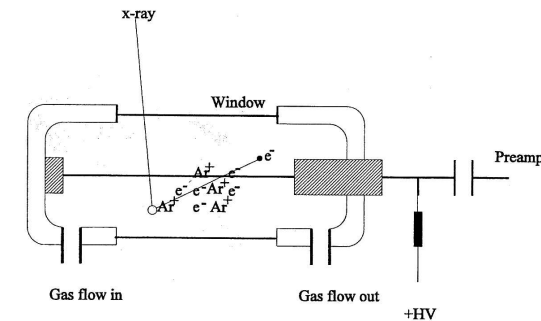
- wavelength scan by varying  $\theta$   
rotation of the crystal with respect to the incoming beam

#### geometric arrangement

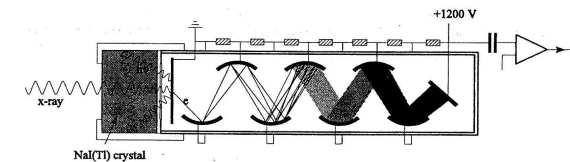


#### detector

flow proportional counter for low energetic X-rays

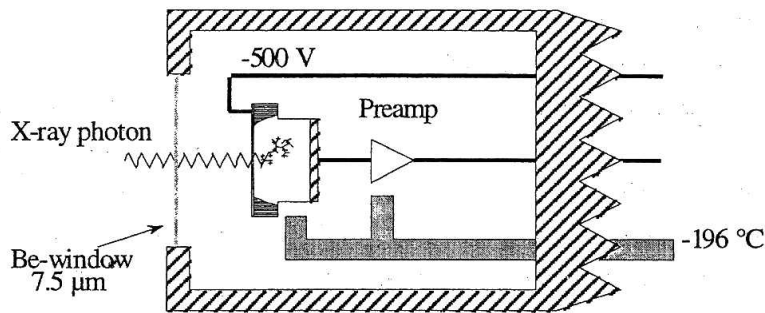


scintillation counter for high energetic X-rays



#### instrumentation – energy dispersive instruments

- energy dispersion and X-ray photon counting in one step
- detector ⊃ semiconductor crystal (Si(Li), hyperpure Ge) at liquid nitrogen temperature ( $-196^{\circ}\text{C}$ )



- incoming X-ray photons create electron hole pairs ⊃ current ⊃ voltage pulse
- the number of electron – hole pairs is proportional to the energy
- best suited for energies  $> 2 \text{ keV}$

#### example

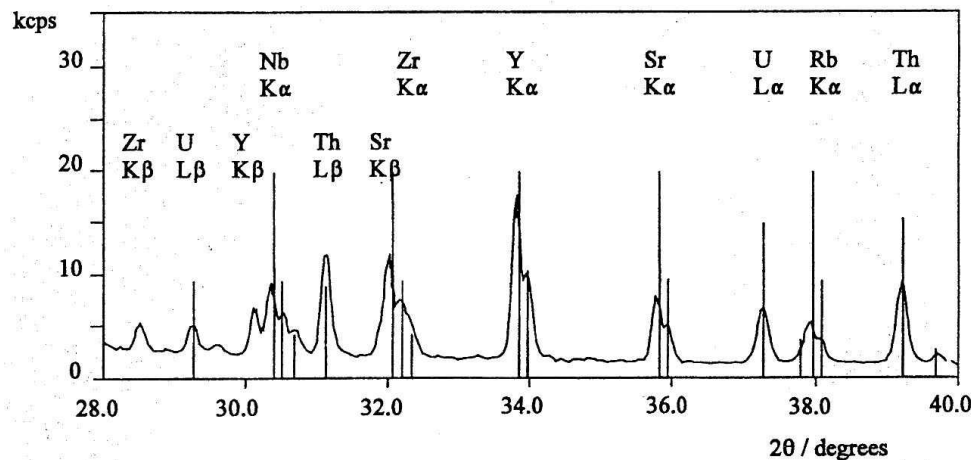
- an Fe K-L<sub>3,2</sub> X-ray photon ( $E=6.400\text{keV}$ ) hits a Si detector
- energy to create 1 electron – hole pair =  $3.85\text{eV}$  ⊃ creation of 1662 ehp's
- the preamplifier converts this current in voltage pulse of e.g.  $32\text{mV}$
- a connected ADC translates the amplified pulse height into a digital number, e.g. 320 ⊃ channel 320 in a memory is increased by 1
- common memories employ 1024 or 2048 channels (0-20 keV and 0 – 40 keV respectively) ⊃ resolution  $\sim 20 \text{ eV}$



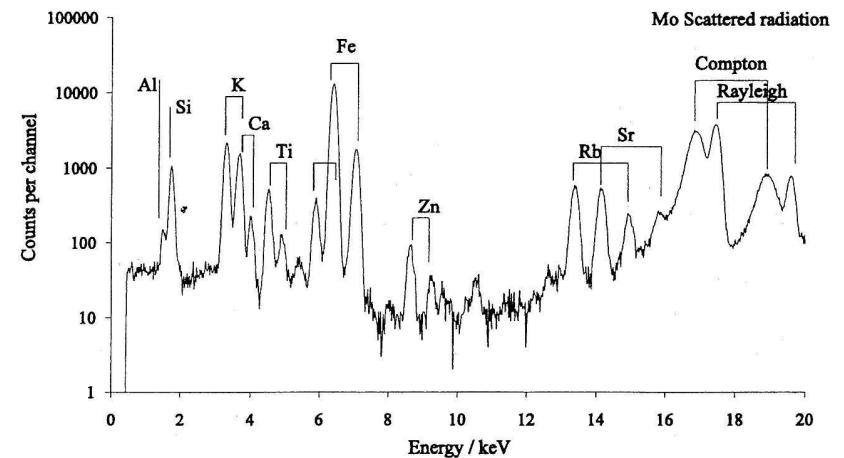
### 2.3.4 X-Ray Fluorescence Spectroscopy

- application of XRF: qualitative and quantitative analysis of elements with  $Z \geq 11$  (F)  
▷ multi-element method
- relatively simple sample preparation  
(bulk solids, pressed powder pellets, fused discs, liquids)
- information depth in the  $\mu\text{m}$  range ▷ homogeneous and smoothed surface required
- qualitative analysis by recording the entire fluorescence spectrum ▷ software assisted element identification by assigning the element specific K, L, M – lines

#### qualitative analysis by XRF



WD-XRF



ED-XRF

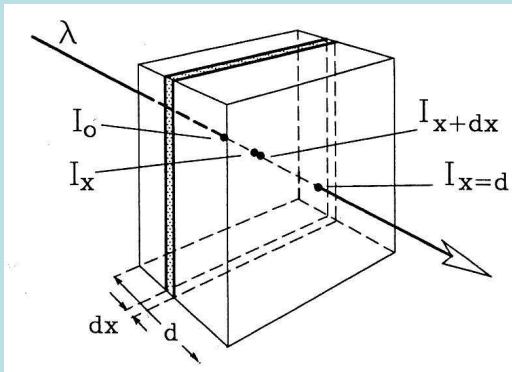


### 2.3.4 X-Ray Fluorescence Spectroscopy

- quantitative analysis requires relation between line intensity and element concentration
- 2 step process:
  - i) determination of the net peak intensity (background subtraction)
  - ii) conversion of the net peak intensity to concentration

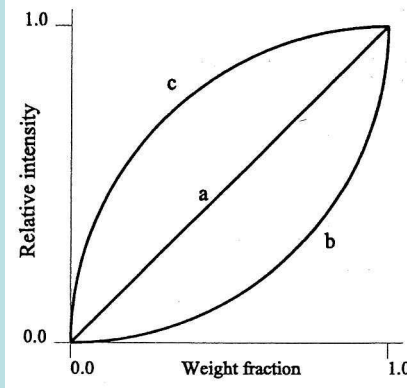
quantitative analysis  
complicated by

#### x-ray attenuation



$$I_x = I_0 \times \exp(-m \times r \times x)$$

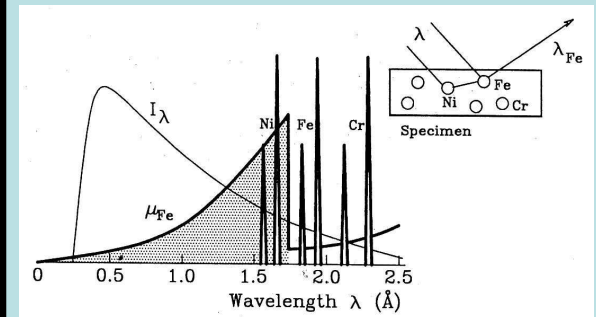
$$m_{sample} = \sum_i a_i c_i m_i$$



- a) no matrix effect
- b) attenuation
- c) enhancement

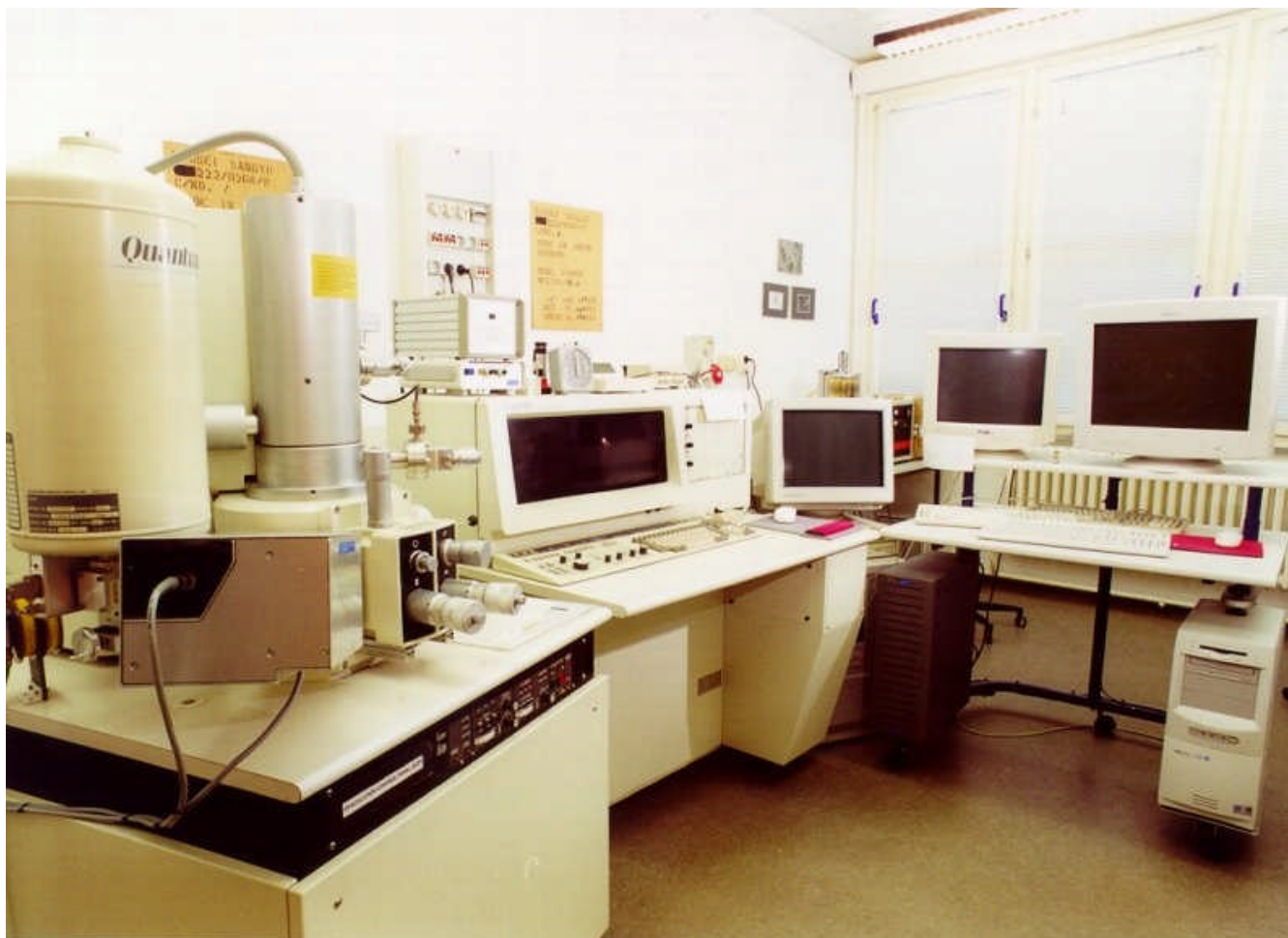
**fundamental parameters  
approach (implemented in  
software)**

#### x-ray enhancement



- excitation of the Fe - K lines by the two Ni - K lines
- observed Fe - K line intensity = sum of primary and secondary fluorescence
- Cr - K line intensity = sum of primary, secondary and tertiary fluorescence

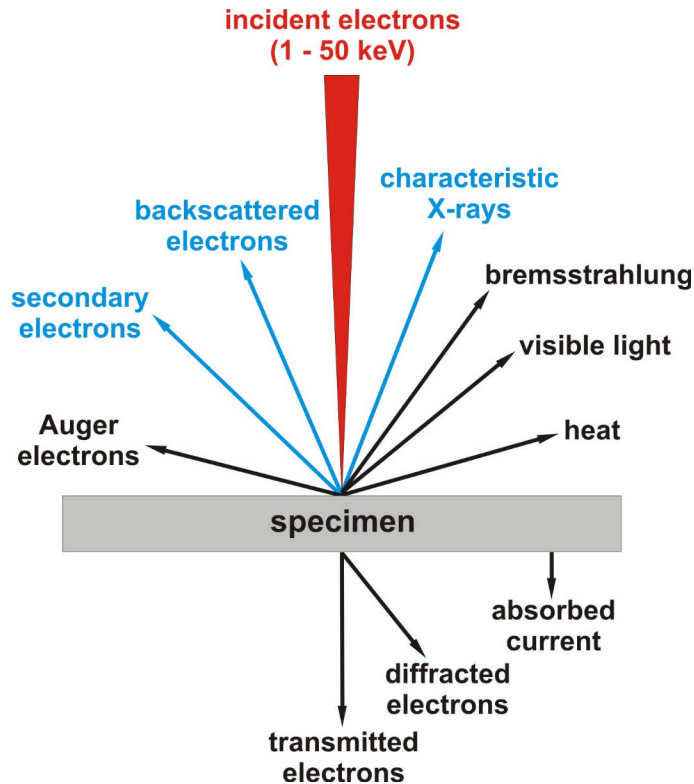
#### EPXMA at the Fritz-Haber-Institute (Inorganic Chemistry Department, Building L)



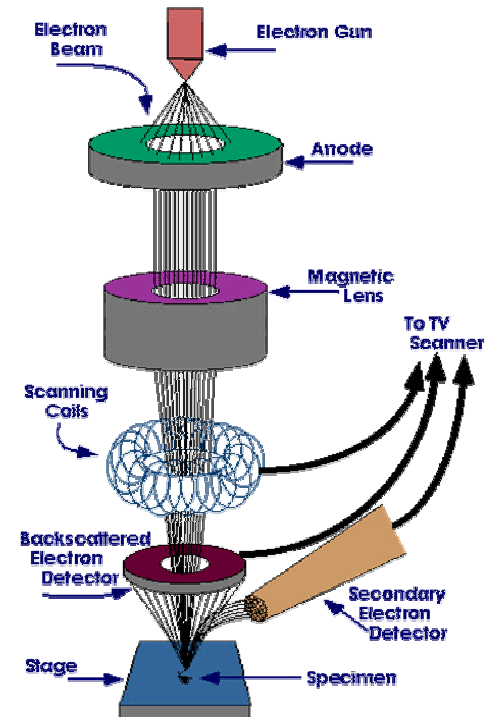
### 2.3.5 Electron Probe X-ray Microanalysis (EPXMA)

- 2D elemental analysis by combination of Scanning Electron Microscopy and X-Ray Fluorescence Analysis

#### electron sample interaction

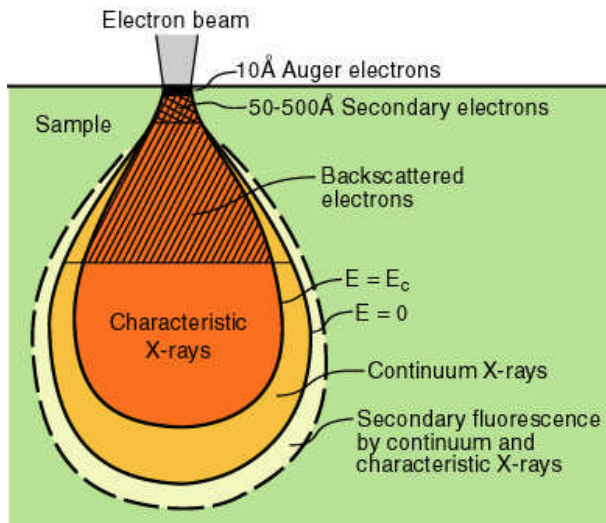


#### SEM instrumentation



- topographic sample image by synchronizing the TV – scanner with the scanning coils
- X-ray detection by a solid – state detector (Si single crystal) as in XRF (not shown above)

#### information depths, spatial resolution

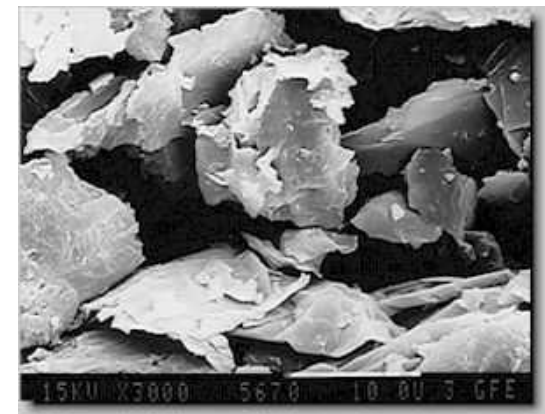


➤ in most cases, the SEM image is created using secondary electrons

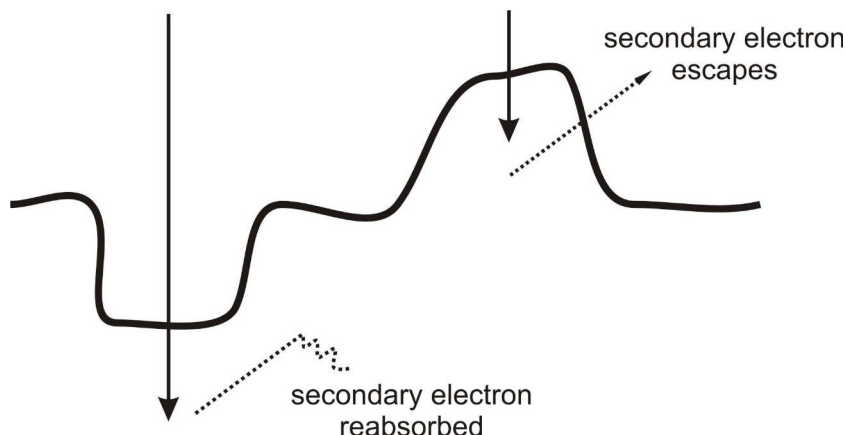
➤ secondary electrons are of low energy ( $< 50\text{eV}$ ), surface sensitive and supply an topographic image of the sample surface

➤ spatial resolution  $< 0.1$  ① possible

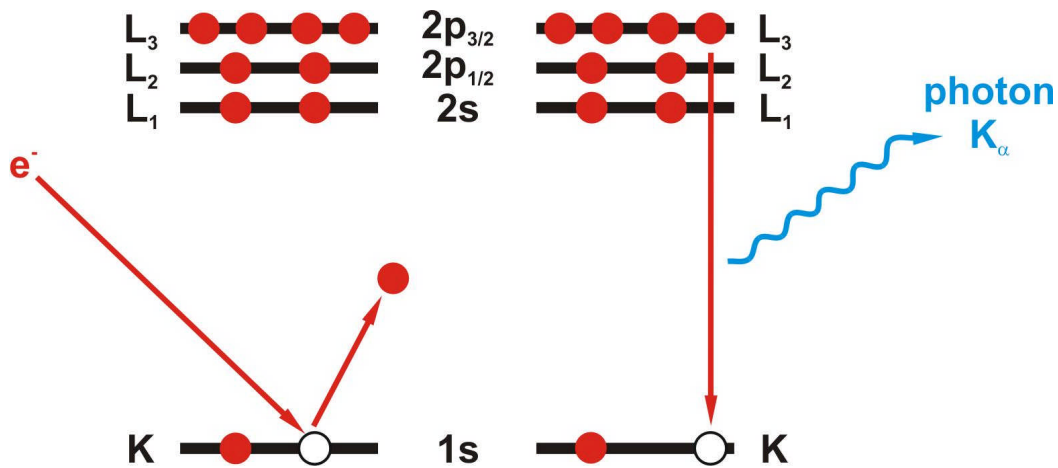
#### secondary electron image



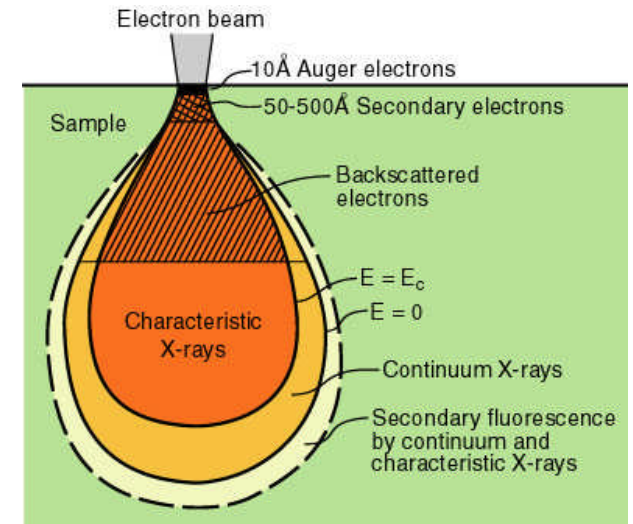
synthetic graphite (25keV,  $\times 3000$ )



#### X – ray generation



#### information depths, spatial resolution



- X-ray generation process similar to XRF
- X-ray spatial resolution much lower than by secondary electrons

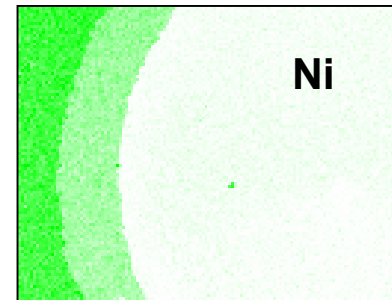
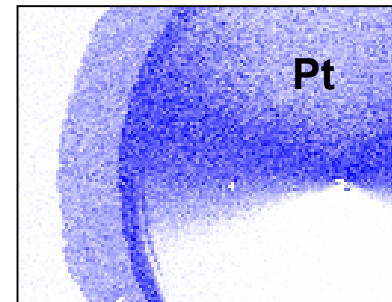
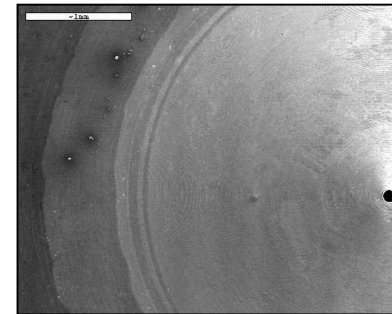


#### analytical performance

- qualitative elemental analysis from  $Z > 11$  by identification of the characteristic KLM peaks (software assisted)
- detection limit  $\sim 1\%$
- minimal sample preparation and sample damage
- quantitative analysis can be performed from element concentrations of 1 – 100% with a relative precision of 1-5%
- similar to XAF, relating net peak intensity with element concentration requires either sophisticated mathematical models (e.g. ZAF correction) or suitable calibration samples

#### example

(pinhole for molecular beam setup)



### 3. Specification of an Analytical Result

- any quantitative analysis relies on a relationship between the measurement value  $y$  and the analyte concentration  $x \Rightarrow y = f(x)$
- if  $y = f(x)$  is known,  $x$  can be calculated by  $x = f^{-1}(y)$
- the mathematical form of  $f(x)$  and  $f^{-1}(y)$  depends on the analytical method

analytical methods			
absolute methods	relative methods		
	definite methods	reference methods	
		direct RM	indirect RM
	$y = b \times x$		$Y = f(x)$
$b = F$	$b = k \times F$	$B = y_r / x_r$	$Y = a + bx$

gravimetry

$$m_{A_q B_p} = \frac{M_{A_q B_p}}{q \times M_A} \times m_A$$

↓  
**B**

photometry

$$A_l = e_l \times d \times c_A$$

↑  
**B**

XPS

$$\frac{I_A}{I_R} = \frac{F_X S(E_k) S(E_k) | (E_k) \cos \theta \times n_A}{F_X S(E_k) S(E_k) | (E_k) \cos \theta \times n_R} = \frac{n_A}{n_R}$$

$$I_A = \frac{I_R}{n_R} \times n_A \rightarrow \mathbf{B}$$

ICP-MS, AES, AAS



### 3. Specification of an Analytical Result

- if the accuracy of the method is assured (e.g. by certified reference materials), the analytical result can be specified as follows

$$x = \bar{x} \pm D\bar{x}$$

$\bar{x}$  = mean of  $n_p$  parallel determinations

$D\bar{x}$  = prediction interval of  $\bar{x}$

- verbal: with a probability of  $P$  is the concentration  $x$  of the analyte  $A$  in the concentration range  $\bar{x} \pm D\bar{x}$
- results from measurements with absolute, definite and direct reference methods can be evaluated using  $n_p$  parallel determinations (entire sample preparation process) and the uncertainties of all values in  $B$  using the rules of error propagation  $\triangleright x = B^{-1} \times y$
- specification of results from measurements with an indirect reference method (experimental calibration) requires to evaluate both the uncertainty of the analysis and of the calibration

### 3. Specification of an Analytical Result

example 1: gravimetric determination of  $\text{Fe}_2\text{O}_3$  in an iron ore

➤ results of  $n_p=5$  parallel determinations 38,71% 38,99% 38,62% 38,74% 38,73%

$$\text{mean: } \bar{x} = \frac{1}{n_p} \sum_i x_i = 38.76\% \quad \text{standard deviation: } s = \sqrt{\frac{\sum_i (x_i - \bar{x})^2}{n_p - 1}} = 0.1381\%$$

degrees of freedom:  $f = n_p - 1 = 4$

confidence level:  $P = 95\%$

t-table

$f$	$P = 0,50$	0,75	0,90	0,95	0,98	0,99
1	1,00	2,41	6,31	12,7	31,82	63,7
2	0,816	1,60	2,92	4,30	6,97	9,92
3	0,765	1,42	2,35	3,18	4,54	5,84
4	0,741	1,34	2,13	2,78	3,75	4,60
5	0,727	1,30	2,01	2,57	3,37	4,03
6	0,718	1,27	1,94	2,45	3,14	3,71

$$\text{result: } \bar{x} \pm D\bar{x} = \bar{x} \pm \frac{s \times t(0.95,4)}{\sqrt{n_p}} = 38.76\% \pm \frac{0.1381\% \times 2.78}{\sqrt{5}} = 38.76\% \pm 0.17\%$$

## example 2: Zn determination by AAS

- calibration:  $m$  samples  $(x_i, y_i) \Rightarrow f = m-2$
- $x_i$  taken as error free
- least squares fit

$$y = \hat{a} + b\hat{x}$$

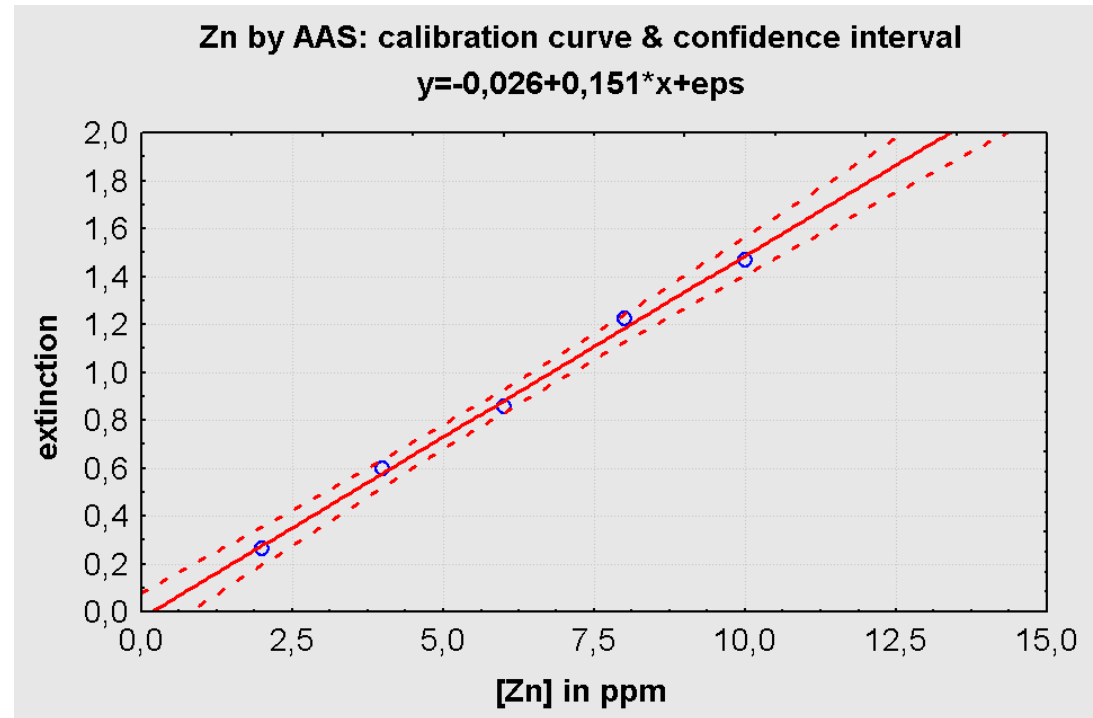
$$\hat{b} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sum_i (x_i - \bar{x})^2}$$

$$\hat{a} = \frac{\sum_i y_i - b \sum_i x_i}{m}$$

$$s_0^2 = \frac{\sum_i (y_i - \hat{y}_i)^2}{m - 2}$$

$$D\hat{y}_k = t(P, f) \sqrt{s_0^2 \frac{1}{m} + \frac{(x_k - \bar{x})^2}{\sum_i (x_i - \bar{x})^2}}$$

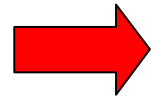
$x_i/\text{ppm}$	2	4	6	8	10
$y_i$ ( $E=\log(I_0/I)$ )	0.266	0.598	0.856	1.222	1.467



#### example 2: Zn determination by AAS

- analysis:  $n_p$  measurement samples (e.g.  $n_p=3$  parallel determinations)

$n_p$	1	2	3
$y_i (E=\log(I_0/I))$	1.064	0.930	0.942

  $\bar{y} = 0.979$

- calculation of  $\bar{x} = \frac{\bar{y} - \hat{a}}{\hat{b}} = \frac{0.979 - (-0.026)}{0.151} = 6.656 \text{ ppm}$

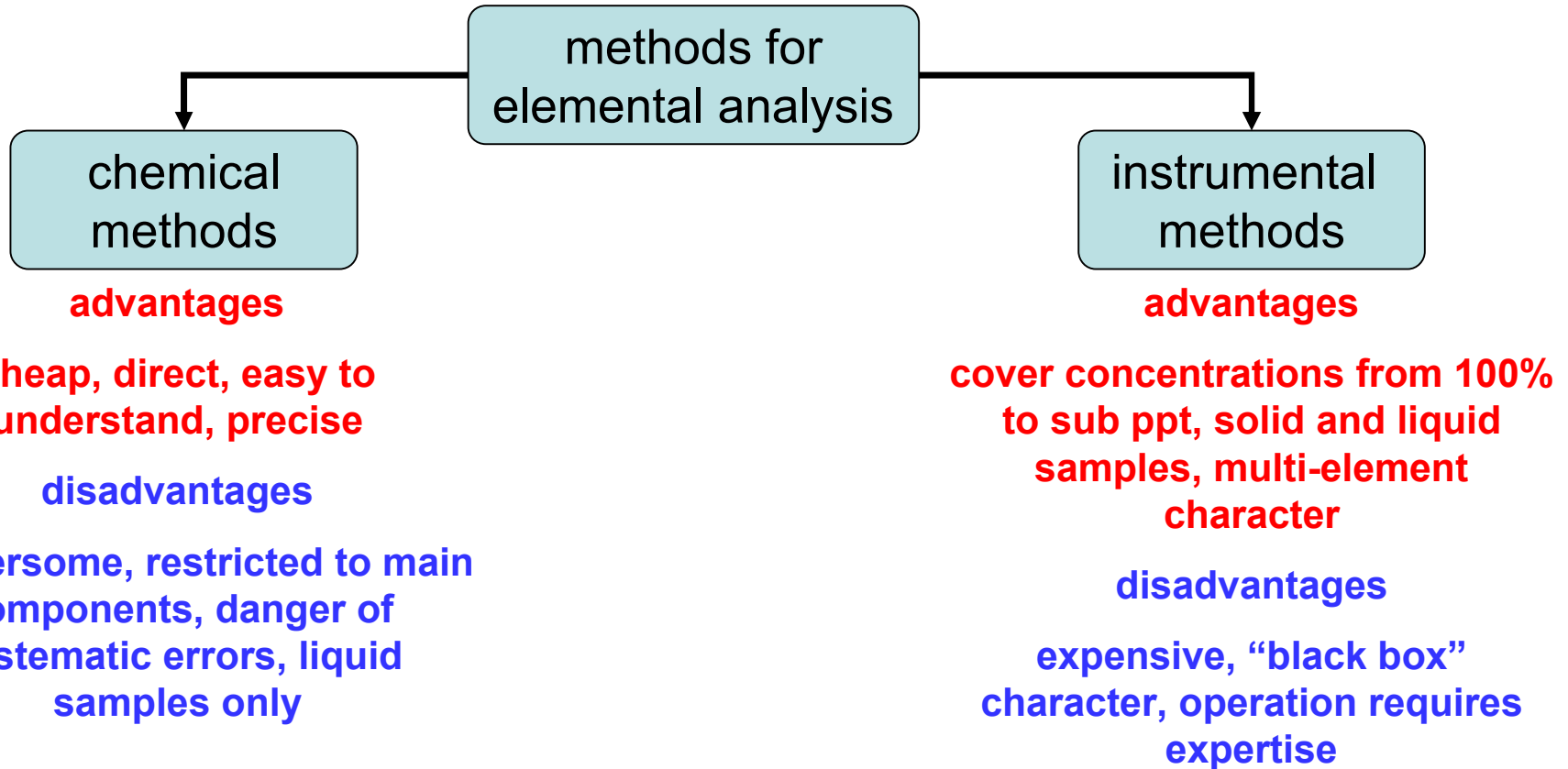
- calculation of  $D\bar{x} = t(P, f) \times \frac{s_0}{\hat{b}} \times \sqrt{\frac{1}{m} + \frac{1}{n_p} + \frac{(\bar{x} - \bar{\bar{x}})^2}{\sum_i \hat{a} (x_i - \bar{\bar{x}})^2}}$

$$D\bar{x} = 3.18 \times \frac{0.0314 \text{ ppm}}{0.151} \times \sqrt{\frac{1}{5} + \frac{1}{3} + \frac{(6.656 - 6)^2 \text{ ppm}^2}{40 \text{ ppm}^2}} = 0.488 \text{ ppm}$$



$$\bar{x} \pm D\bar{x} = 6.656 \pm 0.488 \text{ ppm}$$

- a wide variety of methods are available to determine quantitatively the elemental composition of inorganic samples



- the choice of the right method depends on numerous parameters ( liquid or solid sample, available amount of sample, which and how many elements, expected concentrations, accuracy and precision, decision limit...)

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